Upgraded Petri Net Model and Analysis of Adaptive and Static Arithmetic Coding

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Abstract

In this paper, we analyze several adaptive and static data models of arithmetic compression. These models are represented by using Upgraded Petri net as our original class of the Petri nets. After iterative process of modeling, simulation and analysis, the models are transformed into an application. The models refer to one-pass and two-pass arithmetic coding where set of symbols is refers to bytes or nibbles. Frequency of a symbol is represented as unsigned 32-bit integer. Original software for modeling and simulations of Upgraded Petri net, PeM (Petri Net Manager), is developed and used for all models described in this paper. All models are observed in the experiments by using created application over standard set of files. Experimental results are presented and compared.

Key words: Arithmetic coding, Upgraded Petri nets, data compression, source coding.

1 Introduction

Upgraded Petri nets is a formal mathematical apparatus which enables modeling, simulation and process analysis [17] as is Petri net [11]. We were developed Upgraded Petri nets as new class of Petri nets. These are a graphical and mathematical modeling tool applicable to many systems. Upgraded Petri nets used for describing and studying information processing systems that are characterized as being concurrent, asynchronous, synchronous, distributed, parallel, deterministic, nondeterministic, and/or stochastic as is Petri net. As a graphical tool, Upgraded Petri nets can be used as a visual-communication aid

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similar to flow charts, block diagrams, and networks. Transition firing level, tokens and transition functions are used in these nets to simulate the dynamic and concurrent activities of systems. They enable interactive monitoring of process operations and its gradual improvement from the initial phase, all the way to the final version. We use the Upgraded Petri nets (UPN) which we were developed in order to enable use of Petri nets for hardware modeling, as well as to provide modeling at register level [17], [2]. All models in the paper are created by using UPN. The hierarchical structure of an UPN gives wide possibilities for abstraction. This feature of the UPN provides the model implementation consisting at the same time of elaborate pieces essential for the analysis at a certain level, and also of some general pieces whose details are irrelevant for the analysis at the given level of abstraction [17]. We are using Petri net based simulation via originally developed Petri nets Manager (PeM) software suite. The PeM supports the formal theory of Petri net and also, the formal theory of Upgraded Petri net. It is used for modeling, simulation and analysis of all models shown in the paper. The PeM concurrently fires enabled transitions with respect to the rules of the UPN execution which shown in the next section.

Arithmetic coding maps an input string of data symbols to a code the string in such a way that the original data can be recovered from the code string i.e. it is a form of lossless data compression. Arithmetic coding has been widely used in data compression [18],[10],[3],[4]. This type of coding can encode a sequence from the source at a rate very close to the entropy rate. Arithmetic coding can be easily used in conjunction with sophisticated probability models. The disadvantage of arithmetic coding is its relatively high computational complexity.

In this paper, we consider adaptive and static data model of arithmetic coding. In the work we make Upgraded Petri Nets model, do simulation, and after software implementation of the model we finally do analysis of several data model of adaptive and static arithmetic coding over the standard set of files.

2 Upgraded Petri Nets

In this section, we present Upgraded Petri nets [17], [2] that we were developed in order to enable use of Petri nets for easy modeling of hardware, as well as to provide suitable modeling at register level. Software suite PeM supports: graphic modeling of the Upgraded Petri net, execution of the Upgraded Petri net and reachability tree generation.

2.1 An Upgraded Petri Net Formal Theory

Let \mathbb{N}_0 be the set of non-negative integers, and P and T be disjoint finite nonempty sets of places p_i , $i = 1, \ldots, n$, and transitions t_j , $j = 1, \ldots, m$, respectively, i.e.,

$$P = \{p_1, p_2, \dots, p_n\}, \quad T = \{t_1, t_2, \dots, t_m\}, \quad n, m > 0.$$

A formal theory of Upgraded Petri nets is based on functions as it was introduced in [17]. A Upgraded Petri net is a 9-tuple

$$C = (P, T, F, B, \mu, \theta, TF, TFL, PAF),$$

where

$F: T \times P \to \mathbb{N}_0$	– Input Function,
$B: T \times P \to \mathbb{N}_0$	– Output Function,
$\mu:P\to\mathbb{N}_0$	– Marking Function,
$\theta: T \times \mathbb{N}_0 \to [0, 1]$	– Timing Function,
$TF:T\to \mathbf{A}$	– Transition Function,
$TFL: T \to \mathbb{N}_0$	– Transition Firing Level,
$PAF: P \to (x, y)$	– Place Attributes Function.

The input function assigns a non-negative number to an ordered pair $(t_i, p_j) \in T \times P$. The assigned non-negative integer defines how many times the place p_j is an input with respect to the transition t_i .

The set of places which are input with respect to the transition t_j is presented by ${}^*t_j = \{p_i \in P : F(t_j, p_i) > 0\}$. For a presentation of the place $p_i \in {}^*t_j$ which have the standard input with respect to the t_j , we use the notation ${}^*t_j^S$, and $F^S(t_j, p_i)$ we use for such an input function. For places $p_i \in {}^*t_j$ with inhibitor input with respect to the t_j transition, the notation ${}^*t_j^I$ will be used and $F^I(t_j, p_i)$ for the input function.

The output function maps an ordered pair $(t_i, p_j) \in T \times P$ to the set of nonnegative integers. The assigned non-negative integer shows how many times the place p_i is an output with respect to the t_i transition. A set of places which are output with respect to the t_j transition is presented as follows

$$t_j^* = \{ p_i \in P : B(t_j, p_i) > 0 \}.$$

The marking function assigns a non-negative integer to the p_i place. The marking function can be defined as *n*-dimensional vector (marking): $\mu =$

 $(\mu_1, \mu_2, \ldots, \mu_n)$, where n = |P|. Instead of μ_i it can be used the notation $\mu(p_i)$.

The timing function θ assigns the probability $\lambda_{ij} \in [0, 1]$ to an ordered pair $(t_i, j) \in T \times \mathbb{N}_0$, i.e., $\lambda_{ij} = \theta(t_i, j)$.

The transition function gives an operation $\alpha_j \in A$ to the t_j transition. Here, A denotes the set of operations which can be assigned to the transition.

The firing level function of the transition gives a non-negative integer to the transition t_j . If this number not equals zero, it shows the number of $p_i \in {}^*t_j$ places takes part in the transition firing, and if this number equals zero, then all the places $p_i \in {}^*t_j$ affect the t_j transition firing.

Place attributes function assigns an ordered pair (x, y) to the place p_i . The x component is a real number called x attribute, and y is a non-negative integer called y attribute (i.e., $x \in \mathbb{R}, y \in \mathbb{N}_0$). Over the x attribute belonging to the $p_i \in {}^*t_j$ places, the α_j operation assigned to the t_j transition executes where the order of operands in the operation α_j is defined by the y attributes which belong to the p_i place in accordance to TFL function take part in the transition firing.

An Operation Assigned to a Transition – the function TF assigns to a transition t_j one operation. This operation can be arithmetical operation, logical operation or a file operation [17]. Inside the suite PeM a file which is a target of file operation function has an *.mem extension. This *.mem file is a text file and it is used for simulation of computer system memory. One line inside the *.mem file refers to context of one memory location of computer system that we are modeling.

An arithmetical operation $\alpha_j \in A$, which is assigned to the transition $t_j \in T$, uses attributes x which belong to the places $p_i \in {}^*t_j$ as operands of that operation. A result of an arithmetical operation $\alpha_j \in A$ will be placed into the attributes x which belong to the places $p_i \in t_j^*$. The order of an operand (i.e. order of attributes x which belong to the places $p_i \in {}^*t_j$) in an arithmetical operation $\alpha_j \in A$ is defined by attributes y which belong to the places $p_i \in {}^*t_j$.

A logical operation $\alpha_j \in A$ which is assigned to the transition $t_j \in T$, uses attributes x which belong to the places $p_i \in {}^*t_j$ as operands of that operation. If a result of the logical operation $\alpha_j \in A$ is logical *false* the transition $t_j \in T$ is disabled and will stay in that state until the result of this logical operation $\alpha_j \in A$ becomes logical *true*. The order of an operand (i.e., order of attributes x which belong to the places $p_i \in {}^*t_j$) in a logical operation $\alpha_j \in A$ is defined by attributes y which belong to the places $p_i \in {}^*t_j$. A file operation $\alpha_j \in A$ which is assigned to the transition $t_j \in T$ performs over the context of a file which extension is equal to *.mem. A File Operation $\alpha_j \in A$ addresses context of a *.mem by using attribute x which belongs to the places $p_i \in {}^*t_j$. A result of this operation $\alpha_j \in A$ changes the value of attributes x which belong to the places $p_i \in t_j^*$. The result also can change attributes y which belong to the places $p_i \in t_j^*$, or can change context of addressed line into the *.mem file.

According to a UPN Graph representation we can say the following. The Upgraded Petri Net can be represented via formal mathematical apparatus or graphically. Namely, an UPN is represented by a bipartite multigraph [17] in the same way as a Petri net.

2.2 An Upgraded Petri Net Executing

An Upgraded Petri Net executing represents change of system state from the current state to the next state. This migration from one state to the other one is triggered by firing of the transitions. By UPN executing: marking vector can be changed, contents of *.mem file can be changed, and attributes which belong to the places $p_i \in t_j^*$ of enabled transition t_j can be changed.

A transition $t_j \in T$ can be enabled at the moment $k \in \mathbb{N}_0$ in Upgraded Petri Net [17]: $C = (P, T, F, B, \mu, \theta, TF, TFL, PAF)$ if the next three conditions are satisfied:

- 1° If the timing function $\lambda_{jk} = \theta(t_j, k) > 0$;
- 2° If $TFL(t_j) > 0$ then $(\#p_i(S)) + (\#p_i(I)) = TFL(t_j)$, and if $TFL(t_j) = 0$ then $(\#p_i(S)) + (\#p_i(I)) = |*t_j|$, where $\#p_i(S)$ is a number of places $p_i \in *t_j^S$ such that $\mu(p_i) \ge F^S(t_j, p_i)$, and $\#p_i(I)$ represents a number of places $p_i \in *t_j^I$ for which $\mu(p_i) = 0$;
- 3° If a logical operation $\alpha_j \in A$ assigned to the transition t_j , then the result of the operation α_j must be equal to true.

A marking vector μ will be changed to a new marking vector μ' by firing of transitions t_j , where

$$\mu'(p_i) = \begin{cases} \mu(p_i) - F(t_j, p_i) + B(t_j, p_i), \text{ if } p_i \in {}^*t_j^S, \\ \mu(p_i) + B(t_j, p_i), & \text{ if } p_i \in {}^*t_j^I. \end{cases}$$

By firing of the transition t_j an arithmetic operation is executed or a file operation is executed with respect to the operation that is assigned to t_j by function $TF(t_j)$. A logical operation which assigned to the transition t_j by function $TF(t_j)$ will be executed if the conditions 1° and 2° related to t_j are equal to true.

A conflict in Upgraded Petri Net influences UPN executing. A conflict in UPN is the same as the conflict in Petri-net.

An UPN reachability tree graphically represents all possible marking vectors which can occurs during an UPN execution for given initial marking. Reachability tree shows all states which model can reach from the initial state. The UPN reachability tree is the same as the Petri Net reachability tree.

An UPN executing refers to a concurrent firing of the enabled transitions. An UPN execution generates an UPN flammability tree. This tree is such tree where a node of the tree is a set of the transitions which are enabled at the same time. If there is the same node as the current node in the flammability tree then generating of the flammability tree will be stopped. There are four types of nodes in a flammability tree: root node, double node, dead node, and inner node.

3 Arithmetic Coding

In this section we show some definitions of the basic terms used in the paper and explain how arithmetic coding based on fixed arithmetic works by using integer numbers [9], [6], [16], [8]. We use arithmetic coder in which the range allocated to each symbol is single contiguous interval and no permutations of ranges are applied [16], [7]. There are several approach to the symbol sets and multiple tables in arithmetic coding [19], [1] so we use one symbol set and one coding table.

3.1 Definitions of the some basic terms

The alphabet A_L is a finite, nonempty ordered set. We use mark A_L because of mark A denotes a set of operations which can be assigned to the transition in Upgraded Petri nets. The elements $\{a_1, \ldots, a_n\}$ of an alphabet are called symbols. These elements are distinct ordered. The cardinality of an alphabet A_L will be referred to as $|A_L|$.

We consider a sequence $S = s_1, s_2, \ldots$ of symbols s_i from the alphabet A_L , where $|S| < \infty$.

Let $S = (s_1, \ldots, s_m)$ a finite-length sequence with |S| = m over $A_L = \{a_1, \ldots, a_n\}$.

Let $|S(a_i)|$ refers to the frequency of a_i in S.

Probability of a_i in S is

$$P(a_i) = \frac{|S(a_i)|}{m}.$$

The lower bound Low is the sum of frequencies of all lower symbols than the current symbol. The lower symbols are the symbols which have an index less than the current symbol.

$$Low = \sum_{i=1}^{s-1} Fc_i.$$

The mark s denotes an index of the current symbol while the mark Fc_i is the frequency count of the symbol indexed by i.

The upper bound *High* is a sum of the lower bound and the frequency of the current symbol,

$$High = \sum_{i=1}^{s} Fc_i = Low + Fc_s$$

Total frequencies

$$T_f = \sum_{i=1}^m Fc_i$$

is a sum of all frequencies of the symbols in S.

3.2 Arithmetic coding algorithm

We introduce some basic terms used in arithmetic coding data compression and decompression that will be used in the paper. In this paper we treat this data as binary input stream. A group of such input bits refer to as a symbol. There are two types of symbol that we consider in this work: byte (8 bits) and nibble (4 bits).

The arithmetic coding algorithm works sequentially over the input data stream. We use fixed precision arithmetic, interval expansion and bit-stuffing [18], [12], [13], [15], [14], [5]. Main idea is to output each leading bit as soon as it is known, and then to double the length of the current interval so that it reflects only the unknown part of the final interval. Witten, Neal, and Cleary [18] add a mechanism for preventing the current interval from shrinking too much

when the endpoints are close to the half of the start interval but straddle this half. In that case we do not yet know the next output bit, but we do know that whatever it is, the following bit will have the opposite value; we merely keep track of that fact, and expand the current interval symmetrically about the half of the start interval. This procedure may be repeated any number of times, so the current interval size is always longer than the quarter of the *start interval*.

In this paper start interval, i.e., [Low, High) is initialized to $[0, 2^{31} - 1)$. For each symbol from the input stream two steps will be performed. The first one is subdividing of the current interval into subintervals, one for each symbol from the alphabet. These subintervals are proportional to the frequency of the symbol. The second step is selecting the subinterval regarding to the current symbol from the input stream and setting this interval as the new current interval. At last, we will save leading bits to distinguish the new current interval from further intervals which will be result of interval expansion. The new subinterval is calculated as follows

$$raster = \frac{High - Low + 1}{T_f},\tag{3.1}$$

$$High = Low + raster \cdot \left(\sum_{i=1}^{s} Fc_i\right) - 1, \qquad (3.2)$$

$$Low = Low + raster \cdot \sum_{i=1}^{s-1} Fc_i,$$
(3.3)

where *raster* is a step size of the old subinterval [Low, High) divided by total count of frequencies T_f .

When we encode more and more symbols the *Low* and the *High* converge more and more and in one moment these two values coincide and further encoding will be impossible. To avoid this problem an interval expansion is used. This expansion takes place after the selection of the subinterval. There are four cases of interval expansion process.

The first case is where the subinterval lies entirely within the first half of the *start interval*. In this case we save a zero bit and any 1s left over from previous symbol to the output stream then we will doubled subinterval [Low, High) toward the right. This is e1 scaling.

The second case is where the subinterval lies entirely within the second half of the *start interval*. In this case we save 1 and any 0s left over from previous symbol to the output stream then we will doubled subinterval [Low, High) toward the left. This is e^2 scaling.

The third case is where the subinterval lies entirely within the first quarter and the third quarter of the *start interval*. In this case we keep track of this fact for future output then we will expand subinterval [Low, High) in both directions away from the midpoint of the *start interval*. This is e3 scaling.

The fourth case including all other situations and no expansion will be happened. The expansion process repeats until the fourth case is happened.

In this paper we use that all symbols from S have the initial frequency setup to 1. Also we use an ESC symbol to represent end of coding, so at start of coding |S| = 256 + 1 if a type of symbol is byte or |S| = 16 + 1 if a type of symbol is nibble.

When we decode an input stream main goal is to determine the symbol and update the bounds accordingly. The first task is to determine the interval that contains the symbol then to calculate the code value of the symbol. We use a mark B to denote a buffer which contains encoded stream. The procedure of decoding is to calculate formula (3.1), then to calculate

$$value = \frac{B - Low}{raster},$$

then an encoded symbol will be determined by comparing the *value* to the cumulative frequency count intervals. When the proper interval is found the boundaries will be updated according to the formulas (3.2) and (3.3).

4 Upgraded Petri Net Arithmetic Coding Models

In this section we explain Upgrade Petri Net arithmetic coding models which we developed and used in this paper. The data model used in arithmetic coding can be adaptive or static. In this paper we use both adaptive and static data model.

In this section we will use some abbreviations in our UPN models as follows: B refers to a buffer where input data stream will be loaded, Hf refers to a half of the start interval, FQ refers to a first quarter of the start interval, SC refers to an e3 scaling counter, L refers to Low, H refers to High, ESC refers to the symbol which ends arithmetic coding, and LB refers to bit which is loaded from the input stream.

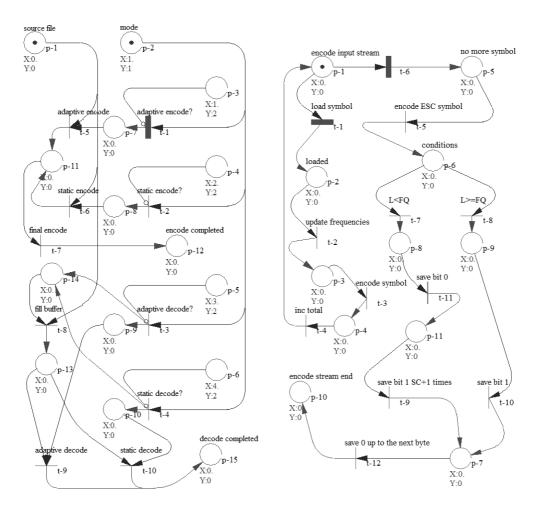


Fig. 1. An UPN model of arithmetic coding compression and decompression (left); An UPN model of adaptive arithmetic coding compression of input stream of symbols (right)

4.1 Adaptive Data Model

Adaptive arithmetic coding is a one-pass procedure where the coder builds up the statistical model while coding the input data.

Fig. 1 (left) shows an UPN model of arithmetic coding compression and decompression at high representation level. Initial marking $\mu(p_1) = \mu(p_2) = 1$ determines a source file which will be compressed or decompressed and compression or decompression mode.

The model refers to two modes of compression and decompression: adaptive and static one. Fig. 1 (left) shows that an adaptive encode is selected, i.e., the transition t_1 is enabled. This UPN model has four possible sequences of transition firing. The first sequence of transition firing is $\{t_1\} - \{t_5\} - \{t_7\}$ and refers to an adaptive encode. The second sequence is $\{t_2\} - \{t_6\} - \{t_7\}$ and refers to a static encode. Transition t_7 refers to final encode for both adaptive and static encode. An event *final encode* will be explained later. The third sequence is $\{t_3\} - \{t_8\} - \{t_9\}$ and refers to an adaptive decode, while the fourth sequence $\{t_4\} - \{t_8\} - \{t_{10}\}$ refers to a static decode. Transition t_8 refers to fill buffer before decode process started.

Fig. 1 (right) shows an UPN model of adaptive arithmetic coding compression at an input stream encode level of representation. Initial marking $\mu(p_1) = 1$ and two enabled transitions t_1 and t_6 refers to two possible cases.

The first case is that there is a symbol in the input stream which we want to encode. A sequence of firing transitions $\{t_1\} - \{t_2\} - \{t_3\} - \{t_4\}$ occurs. This sequence refers to symbol loaded, then, update table of frequencies, then encode the symbol, then increment a total of encoded symbols and finally check again is there another symbol in input steam.

The second case is that there are no more symbols in input stream. Sequence of firing transitions $\{t_6\} - \{t_5\}$ encodes *ESC* symbol and checks *Low* value.

If this value is less than the first quarter of the start interval a sequence $\{t_7\} - \{t_{11}\} - \{t_9\} - \{t_{12}\}$ occurs. This sequence saves bit 0, then saves bit 1 SC + 1 times, then saves bit 0 and finally by firing of the transition t_{12} the output stream is populated by zeros up to the next byte.

On the other side, if the Low value is greater than or equal to the first quarter of the coding interval a sequence $\{t_8\} - \{t_{10}\}$ occurs. This sequence saves bit 1. At last, transition t_{12} is enabled. By firing of this transition the output stream is populated by zeros up to the next byte.

All savings we were mentioned in the sections refers to the output stream.

Fig. 2 (left) shows an UPN model of adaptive arithmetic coding compression at a symbol encode level of representation. Initial marking $\mu(p_1) = 1$ determines that an sequence of transition firing $\{t_1\} - \{t_2\} - \{t_3\}$ occurs. This sequence calculated *Low* value (denoted as L mark on the figure), then calculated *High* value (denoted as H mark on the figure) and checks conditions for: e1 scaling, e2 scaling and for e3 scaling update.

Condition for e1 scaling is that *High* less than half of the coding interval value. Condition for e2 scaling is that *Low* is greater than or equal to a half of the coding interval. Condition for e3 scaling update is that *Low* is greater than or equal to the first quarter of the coding interval and that *High* is less than the third quarter of the interval value.

A sequence $\{t_4\} - \{t_7\} - \{t_9\} - \{t_{11}\}$ does e1 scaling: saves bit 0, then recal-

culated values:

$$Low = 2 \cdot Low, \quad High = 2 \cdot High + 1,$$
 (4.4)

and then saves bit $1 e^3$ scaling counter (SC) times.

A sequence $\{t_5\} - \{t_8\} - \{t_{10}\} - \{t_{12}\}$ does e2 scaling: saves bit 1, then concurrently recalculated values:

$$Low = 2 \cdot (Low - Hf), \quad High = 2 \cdot (High - Hf) + 1, \tag{4.5}$$

than saves bit $0 e^3$ scaling counter (SC) times.

After anyone of the last two sequences a set of transitions $\{t_{13}, t_{18}\}$ is enabled. At this moment only one of these transitions will be activated because of $\mu(p_{11}) = 1$ and according to the conditions 1°, 2° and 3°.

Firing of transition t_{13} changes marking $\mu(p_{12}) = 1$ which represents end of a symbol encoding. Firing of the transition t_{18} starts an new iteration of checking conditions for e1, e2 or e3 scaling. Firing of the transition t_4 refers that e1 scaling condition is true and e1 scaling starts again, while firing of transition t_5 refers that e2 scaling condition is true and e2 scaling starts again. Firing of transition t_6 means that e3 scaling update condition is true and activates e3 scaling update. This model shows that after e1 scaling loop or e2 scaling loop follows checking of e3 scaling update condition.

The update e3 scaling sequence is $\{t_6\} - \{t_{14}, t_{15}, t_{16}\}$. This sequence can do three parallel things: increments e3 scaling counter (SC), and calculates

$$Low = 2 \cdot (Low - FQ)$$
 and $High = 2 \cdot (High - FQ) + 1.$ (4.6)

After this sequence of transition firing two transitions $\{t_{17}, t_{19}\}$ are enabled. At this moment only one of these transitions will be activated because of $\mu(p_{14}) = 3$ and according to the conditions 1°, 2° and 3°. By firing of the transition t_{19} the state of the net goes to the new iteration of e3 scaling update.

The second case is that transition t_{17} will be activated and this means the end of the symbol encoding.

Fig. 2 (right) shows an UPN model of adaptive arithmetic coding decompression at an input stream level of representation.

Initial marking $\mu(p_1) = 1$ determines that an sequence of transition firing $\{t_1\} - \{t_2\} - \{t_3\} - \{t_4\}$ occurs. This sequence fill coding buffer from the input stream and calculates raster (we split number space into single step), after that

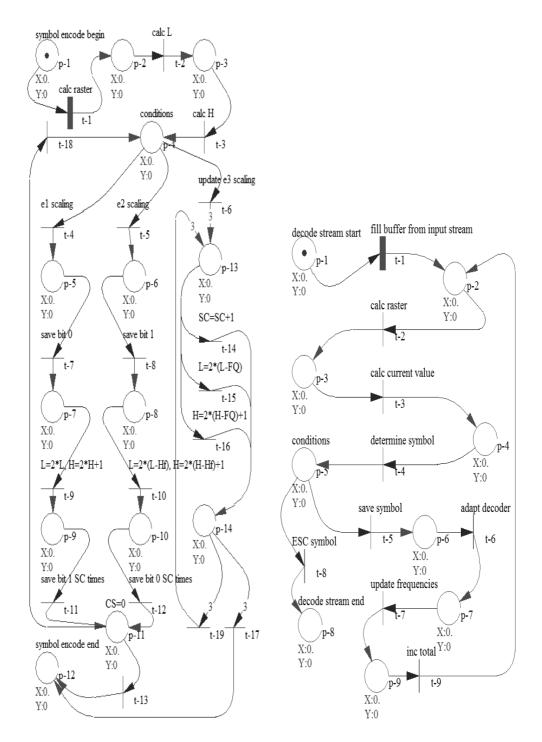


Fig. 2. An UPN model of adaptive arithmetic coding compression which refers to a symbol encode (left); An UPN model of adaptive arithmetic coding decompression of a input stream (right)

current value will be calculated and finally the symbol will be determined. At this moment $\mu(p_1) = 1$ and two transitions t_5 and t_8 are enabled. Only one of these transitions will be activated according to conditions 1° , 2° and 3° . Now we have two cases.

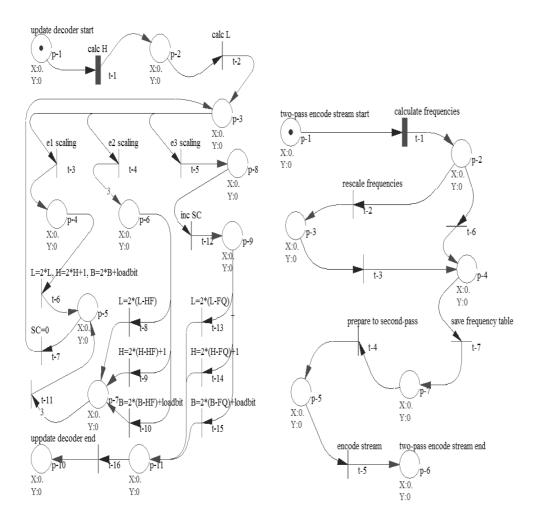


Fig. 3. An UPN model of adaptive arithmetic coding decompression which refers to an update of the decoder (left); An UPN model of two-pass static arithmetic coding compression (right)

The first case is a sequence of transitions firing $\{t_5\} - \{t_6\} - \{t_7\} - \{t_9\}$ which saves the symbol, than adapt decoder, then update frequencies, then increment total of saved symbols and finally goes to calculates raster again. Now the sequence $\{t_2\} - \{t_3\} - \{t_4\}$ occurs as mentioned earlier, i.e., a new iteration of encoding symbol starts again.

The second case is a firing of transition t_8 which represents and of a decoding of the input stream. This means that the *ESC* symbol is decoded from the input stream.

Fig. 3 (left) shows an UPN model of adaptive arithmetic coding decompression which refers to an update of the decoder. Initial marking $\mu(p_1) = 1$ determines that an sequence of transition firing $\{t_1\} - \{t_2\}$ occurs. This sequence calculates values in order *High* then *Low* according to formulas (3.2), (3.3).

At this moment $\mu(p_3) = 1$ and this state of model checks conditions for: e_1

scaling, e^2 scaling and for e^3 scaling. Condition for e^1 scaling is that *High* less than half of the coding interval value. Condition for e^2 scaling is that *Low* is greater than or equal to a half of the coding interval. Condition for e^3 scaling update is that *Low* is greater than or equal to the first quarter of the coding interval and that *High* is less than the third quarter of the interval value.

The first case is a sequence of transition firing $\{t_3\} - \{t_6\} - \{t_7\}$. This sequence refers to e1 scaling, and it calculates concurrently values *Low* and *High* according to formulas (4.4), then update buffer B:

$$B = 2 \cdot B + LB,$$

then set e3 scaling counter (SC) to zero, and finally goes into the new iteration cycle by setting $\mu(p_3) = 1$.

The second case is a sequence of transition firing $\{t_4\}-\{t_8, t_9, t_{10}\}-\{t_{11}\}-\{t_7\}$. This sequence concurrently calculates three values: Low and High according to formulas 4.5 and buffer

$$B = 2 \cdot (B - Hf) + LB.$$

Before firing of the transition t_{11} marking $\mu(p_7) = 3$ and $\mu(p_5) = 0$ while the marking after firing of the transition t_{11} will become $\mu(p_7) = 0$ and $\mu(p_5) = 1$. It saves number of tokens in the net. At last, the sequence set e_3 scaling counter (SC) to zero. After this by setting $\mu(p_3) = 1$ the new iteration cycle of conditions checking starts.

The third case is a sequence of transition firing $\{t_5\} - \{t_{12}\} - \{t_{13}, t_{14}, t_{15}\} - \{t_{16}\}$. The sequence increments counter of e3 scaling (SC) then concurrently calculates values Low and High according to the formulas (4.6) and buffer

$$B = 2 \cdot (B - FQ) + LB \, .$$

After this firing of the transition t_{16} saves number of tokens in this net as in the previous case and set new state of the model which means the end of the update decoder.

4.2 Static Data Model

Static arithmetic coding uses two passes or use fixed statistical models and perform only one-pass over the data. In two-pass case the first pass makes statistical model. The second pass compresses the data. This reduces the total

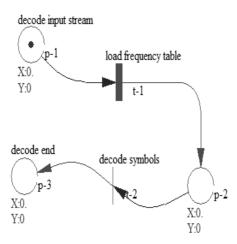


Fig. 4. An UPN model of arithmetic coding decompression of static encoded input stream

compression coding efficiency because this statistical model has to be transmitted to the decoder.

Fig. 3 (right) shows an UPN model of two-pass static arithmetic compression at an input stream level of representation. Initial marking $\mu(p_1) = 1$ determines that transition t_1 is enabled and will be fired. This firing calculates frequencies of the symbol over the input stream. The state of the UPN model is $\mu(p_2) = 1$ and there are two enabled transitions t_2 and t_6 . Only one of these transitions will be fired according to the conditions 1° , 2° and 3° .

The first case is that the transition t_2 will be fired. This means that UPN model rescales the frequencies. After this transition t_3 is enabled and will be fired and now is $\mu(p_4) = 1$.

The second case is that transition t_6 will be fired, and this firing also sets $\mu(p_4) = 1$. The second case avoids frequency rescaling.

After both of these cases a sequence of transition firing $\{t_7\} - \{t_4\} - \{t_5\}$ occurs. This sequence saves frequency table to the output stream, then prepares second pass of encoding (update pointers to the input steam), then decode input stream by using the frequency table.

Fig. 4 shows an UPN model of arithmetic coding decompression of static encoded input stream. This very simple model represents an initial marking $\mu(p_1) = 1$ which makes a sequence of transition firing $\{t_1\} - \{t_2\}$. This sequence loads frequency table from begin of the input stream by using data and then decode rest of data which represent encoded symbols. By executing the UPN model for given initial marking shown in Fig. 1 (left) the next sequence of transitions firing will happen $\{t_1\} - \{t_5\} - \{t_7\}$ and appropriate sequence of marking vectors is:

(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = (initial marking),(1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) = (dead node).

A dead node presents a state when there are no enabled transitions in the net.

Other possible cases are determined by value of $p_2 x$ (means attribute x of the place p_2) as follows:

 $p_2 \cdot x = 2$ determines the sequences $\{t_2\} - \{t_6\} - \{t_7\}$ and

(1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = (initial marking),(1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) = (dead node).

 $p_{2}x = 3$ determines the sequences $\{t_3\} - \{t_8\} - \{t_9\}$ and

 $p_2 x = 4$ determines the sequences $\{t_4\} - \{t_8\} - \{t_{10}\}$ and

By executing the UPN model for given initial marking shown in Fig. 1 (right) the next sequences of transitions firing will happen:

Sequence 2.1: $\{t_1\} - \{t_2\} - \{t_3\} - \{t_4\}$ and appropriate sequence of marking vectors is as follows:

(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(initial marking), (0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0), (0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0), (1, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(double node, init. marking).

Sequence 2.2: $\{t_6\} - \{t_5\} - \{t_7\} - \{t_{11}\} - \{t_9\} - \{t_{12}\}$ and appropriate sequence of marking vectors is as follows:

(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = (initial marking),(0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0) = (dead node).

Sequence 2.3: $\{t_6\} - \{t_5\} - \{t_8\} - \{t_{10}\} - \{t_{12}\}$ and appropriate sequence of marking vectors is as follows:

((1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = (initial marking),(0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 1, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 1, 0) = (dead node).

By executing the UPN model for a given initial marking shown in Fig. 2 (left), the next sequences (mark this as 3.1) of transitions firing will happen $\{t_1\} - \{t_2\} - \{t_3\}$ and appropriate sequence of marking vectors is:

 $1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = \text{(initial marking)}, \\(0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0), \\(0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0), \\(0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0).$

There are several sequences that will be possible from this net state as follows (mark them as 3.2.1, 3.2.2 and 3.2.3, respectively):

Sequence 3.2.1: $\{t_4\} - \{t_7\} - \{t_9\} - \{t_{11}\}$ and appropriate sequence of marking vectors is as follows:

(0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(will be double node), (0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0), (0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) =(double node).

Sequence 3.2.2: $\{t_5\} - \{t_8\} - \{t_{10}\} - \{t_{12}\}$ and appropriate sequence of marking vectors is as follows:

(0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(will be double node), (0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0), (0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0), (0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) =(double node).

From this double node which appears also at the end of the sequence 3.2.1 there are two possible sequences.

The first one is $\{t_{18}\}$ with its appropriate sequence of marking vectors is as follows:

(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) =(double node), (0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(double node).

The second one is $\{t_{13}\}$ and appropriate sequence of marking vectors is as follows:

(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) =(double node), (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0) =(dead node).

Sequence 3.2.3 includes two cases. The first one is a sequence $\{t_6\}-\{t_{16}\}-\{t_{19}\}$ and appropriate sequence of marking vectors is as follows:

(0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(double node), (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0) =(will be double node), (0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0) =(double node).

These marking vectors include the cyclic sequence $\{t_{16}\} - \{t_{19}\}$. The second sequence is a sequence $\{t_6\} - \{t_{16}\} - \{t_{17}\}$ and appropriate sequence of marking vectors is as follows:

(0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) = (double node),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0) = (double node),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1) = (double node),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0) = (dead node). By executing the UPN model for given initial marking shown in Fig. 2 (right) the two sequences of transitions firing will happen.

The first one $\{t_1\} - \{t_2\} - \{t_3\} - \{t_4\} - \{t_8\}$ and appropriate sequence of marking vectors is:

(1, 0, 0, 0, 0, 0, 0, 0, 0) =(initial marking), (0, 1, 0, 0, 0, 0, 0, 0, 0) =(will be double node), (0, 0, 1, 0, 0, 0, 0, 0, 0), (0, 0, 0, 1, 0, 0, 0, 0, 0), (0, 0, 0, 0, 1, 0, 0, 0, 0), (0, 0, 0, 0, 0, 0, 0, 1, 0) =(dead node).

The second one $\{t_1\} - \{t_2\} - \{t_3\} - \{t_4\} - \{t_5\} - \{t_6\} - \{t_7\} - \{t_9\}$ and appropriate sequence of marking vectors is:

(1, 0, 0, 0, 0, 0, 0, 0, 0) = (initial marking),(0, 1, 0, 0, 0, 0, 0, 0, 0) = (will be double node),(0, 0, 1, 0, 0, 0, 0, 0, 0),(0, 0, 0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 0, 0, 1, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 1),(0, 1, 0, 0, 0, 0, 0, 0, 0) = (double node).

By executing the UPN model for given initial marking shown in Fig. 3 (left) the sequence of transitions firing $\{t_1\} - \{t_2\}$ will happen and appropriate sequence of marking vectors is:

(1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) =(initial marking), (0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0), (0, 0, 1, 0, 0, 0, 0, 0, 0, 0) =(will be double node).

There are three sequences possible from this state. The first one is $\{t_3\} - \{t_6\} - \{t_7\}$ and appropriate sequence of marking vectors is:

(0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0) = (will be double node), (0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0), (0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0) = (will be double node), (0, 0, 1, 0, 0, 0, 0, 0, 0, 0) = (double node).

The second sequence is $\{t_4\} - \{t_8, t_9, t_{10}\} - \{t_{11}\}$ and appropriate sequence of marking vectors is:

(0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0) = (double node),(0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 0, 1, 0, 0, 0, 0, 0) = (double node).

The third sequence is $\{t_5\} - \{t_{12}\} - \{t_{13}, t_{14}, t_{15}\} - \{t_{16}\}$ and appropriate sequence of marking vectors is:

(0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0) = (double node),(0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0),(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1) = (dead node).

By executing the UPN model for given initial marking shown Fig. 3 (right) the two sequences of transitions firing will happen. The first sequence is $\{t_1\} - \{t_2\} - \{t_3\} - \{t_7\} - \{t_4\} - \{t_5\}$ and appropriate sequence of marking vectors is:

(1, 0, 0, 0, 0, 0, 0) = (initial marking),(0, 1, 0, 0, 0, 0, 0),(0, 0, 1, 0, 0, 0, 0),(0, 0, 0, 1, 0, 0, 0),(0, 0, 0, 0, 0, 0, 1),(0, 0, 0, 0, 0, 1, 0, 0),(0, 0, 0, 0, 0, 1, 0) = (dead node).

The second sequence is $\{t_1\}-\{t_6\}-\{t_7\}-\{t_4\}-\{t_5\}$ and appropriate sequence of marking vectors is:

(1, 0, 0, 0, 0, 0, 0) = (initial marking),(0, 1, 0, 0, 0, 0, 0),(0, 0, 0, 1, 0, 0, 0),(0, 0, 0, 0, 0, 0, 1),(0, 0, 0, 0, 0, 1, 0, 0),(0, 0, 0, 0, 0, 1, 0) = (dead node).

By executing the UPN model for given initial marking shown in Fig. 4 a trivial sequence of transitions firing will happen: $\{t_1\} - \{t_2\}$ and appropriate sequence of marking vectors is: (1, 0, 0, 0, 0, 0, 0) = (initial marking); (0, 1, 0, 0, 0, 0, 0); (0, 0, 1, 0, 0, 0, 0) = (dead node).

5 Experimental Results

According to all UPN models shown in this paper an application is created. The application compresses and decompresses several set of test files [20] by using arithmetic coding with respect to the input parameters. These input parameters are: symbol type (byte or nibble), adaptive or static data model and frequency scaling (scaled or non-scaled). If we use frequency scaled option there are two cases: frequency table divide by 2 and proportional scaling frequency table from min frequency equals 1 to max frequency equals 255. In all possible cases of our arithmetic coding initial (minimum) frequency for all symbols is 1.

In this section we use some abbreviations for various types of arithmetic coding which depend on these input parameters. These abbreviations are as follows:

- *Type_*10 represents that an input symbol is a byte, we use adaptive arithmetic coding with non-scaled frequency table;
- *Type_*11 represents that an input symbol is a byte, we use adaptive arithmetic coding with divby2-scaled frequency table;
- Type_12 represents that an input symbol is a byte, we use adaptive arithmetic coding with max255-scaled frequency table;
- *Type_*20 represents that an input symbol is a byte, we use static arithmetic coding with non-scaled frequency table;
- *Type_*21 represents that an input symbol is a byte, we use static arithmetic coding with divby2-scaled frequency table;
- *Type_*22 represents that an input symbol is a byte, we use static arithmetic coding with max255-scaled frequency table;
- *Type_*30 represents that an input symbol is a nibble, we use adaptive arithmetic coding with non-scaled frequency table;
- *Type_*31 represents that an input symbol is a nibble, we use adaptive arithmetic coding with divby2-scaled frequency table;
- *Type_*32 represents that an input symbol is a nibble, we use adaptive arithmetic coding with max255-scaled frequency table;
- *Type_*40 represents that an input symbol is a nibble, we use static arithmetic coding with non-scaled frequency table;
- *Type_*41 represents that an input symbol is a nibble, we use static arithmetic coding with divby2-scaled frequency table;
- *Type_*42 represents that an input symbol is a nibble, we use static arithmetic coding with max255-scaled frequency table;

The main goal in this experiment is to verify UPN models transformed into the real application and to explore our 12 types of arithmetic coding compression over the used test files [20].

Table 5.1

File sizes (bytes) in arithmetic coding compression *Type*_10, *Type*_11, *Type*_12; *Type*_20, *Type*_21, *Type*_22 over texture files

Name of tiff file	e & its size	$Type_10$	$Type_11$	$Type_12$	$Type_20$	$Type_21$	$Type_22$
texmos1.p512	262,278	$259,\!557$	259,591	259,597	260,418	260,415	260,414
texmos2.p512	262,278	$254{,}538$	$254,\!584$	$254,\!589$	$255,\!394$	$255,\!392$	$255,\!404$
texmos2.s512	262,278	98,886	$99,\!177$	105,951	99,602	$99,\!641$	105,227
texmos3.p512	262,278	255,917	255,952	255,950	256,775	256,772	256,777
texmos3.s512	262,278	98,358	$98,\!644$	108,202	99,073	99,113	$105,\!874$
texmos3b.p512	262,278	255,924	255,960	255,958	256,782	256,779	256,784
1.3.01	1,048,710	975,783	975,809	975,924	976,626	$976,\!582$	976,810
1.3.02	1,048,710	965,618	965,666	965,958	966,459	966,416	966,699
1.3.03	1,048,710	956,633	956,712	957,079	957,466	957,425	957,751
1.3.04	1,048,710	953,032	953,057	$953,\!285$	953,882	953,836	$953,\!935$
1.3.05	1,048,710	999,535	999,545	999,533	$1,\!000,\!392$	1,000,346	1,000,354

Table 5.2

File sizes (bytes) in arithmetic coding compression *Type_30*, *Type_31*, *Type_32*; *Type_40*, *Type_41*, *Type_42* over texture files

Name of tiff t	file & its size	$Type_{-}30$	$Type_31$	$Type_32$	$Type_40$	$Type_41$	$Type_42$
texmos1.p512	$262,\!278$	262,259	262,254	262,272	262,318	262,307	$262,\!319$
texmos2.p512	262,278	262,144	262,139	$262,\!158$	262,203	$262,\!192$	262,205
texmos2.s512	262,278	173,773	173,787	$175,\!391$	$173,\!827$	$173,\!815$	$175,\!059$
texmos3.p512	$262,\!278$	$262,\!153$	$262,\!150$	262,169	262,213	262,202	262,214
texmos3.s512	262,278	98,358	$98,\!644$	108,202	172,782	172,771	174,038
texmos3b.p512	2 262,278	$262,\!156$	$262,\!152$	$262,\!171$	262,215	262,203	262,216
1.3.01	1,048,710	1,020,475	1,020,385	1,020,425	1,020,705	1,020,520	1,020,485
1.3.02	1,048,710	1,014,635	1,014,546	1,014,652	1,014,869	1,014,682	1,014,667
1.3.03	1,048,710	1,012,663	1,012,572	1,012,669	1,012,891	1,012,708	1,012,684
1.3.04	1,048,710	1,007,214	1,007,125	1,007,247	1,007,445	1,007,260	1,007,259
1.3.05	1,048,710	$1,\!030,\!220$	1,030,130	1,030,163	$1,\!030,\!443$	1,030,263	1,030,209

The first two tables (Tables 5.1 and 5.2) show experimental results which refer to arithmetic coding compression of some test texture files [20]. The compressed files shown in Table 5.1 (second part) include appropriate frequency table which is 1024 bytes long because of byte input symbol. The compressed files shown on Table 5.2 (second part) include appropriate frequency table which is 64 bytes long because of nibble input symbol.

The next two tables (Tables 5.3 and 5.4) show experimental results refer to arithmetic coding compression of some test aerial files [20]. The compressed files shown on Table 5.3 (second part) include appropriate frequency table which is 1024 bytes long (byte input symbol). The compressed files shown on Table 5.4 (second part) include appropriate frequency table which is 64 bytes long (nibble input symbol).

Finally, the last two tables (Table 5.5 and 5.6) show experimental results which refer to arithmetic coding compression of some test misc files [20]. The compressed files shown on Table 5.5(second part) include appropriate fre-

Table 5.3

File sizes (bytes) in arithmetic coding compression *Type*_10, *Type*_11, *Type*_12; *Type*_20, *Type*_21, *Type*_22 over aerial files

Name of file	& its size	$Type_{10}$	$Type_11$	$Type_{12}$	$Type_20$	$Type_21$	$Type_22$
2.1.02.tiff	$786,\!572$	721,177	721,273	721,515	722,008	721,986	722,113
2.1.08.tiff	$786,\!572$	628,095	628,248	$629,\!552$	$628,\!878$	$628,\!866$	$630,\!392$
2.1.12.tiff	$786,\!572$	646, 185	$646,\!309$	$646,\!309$	646,972	$646,\!960$	648,214
2.2.03.tiff	$3,\!145,\!868$	$2,\!490,\!157$	$2,\!490,\!183$	$2,\!499,\!028$	2,491,287	$2,\!490,\!883$	$2,\!497,\!750$
2.2.13.tiff	$3,\!145,\!868$	$2,\!892,\!415$	$2,\!892,\!309$	$2,\!892,\!888$	$2,\!893,\!595$	$2,\!893,\!186$	$2,\!893,\!682$
2.2.17.tiff	$3,\!145,\!868$	2,799,801	$2,\!799,\!744$	$2,\!801,\!846$	$2,\!800,\!959$	$2,\!800,\!548$	$2,\!802,\!071$
2.2.24.tiff	$3,\!145,\!868$	$2,\!884,\!736$	$2,\!884,\!641$	$2,\!885,\!452$	2,885,915	$2,\!885,\!502$	$2,\!886,\!077$
3.2.25.tiff	1,048,710	883,060	883,204	884,926	883,866	883,830	$885,\!451$

Table 5.4

File sizes (bytes) in arithmetic coding compression *Type_30*, *Type_31*, *Type_32*; *Type_40*, *Type_41*, *Type_42* over aerial files

Name of file	& its size	$Type_{-30}$	$Type_31$	$Type_32$	$Type_40$	$Type_41$	$Type_42$
2.1.02.tiff	786,572	759,655	759,606	759,707	759,805	759,701	759,716
2.1.08.tiff	$786,\!572$	$714,\!532$	$714,\!482$	$714,\!672$	714,681	$714,\!578$	714,730
2.1.12.tiff	786,572	725,919	$725,\!870$	726,020	726,071	$725,\!965$	726,084
2.2.03.tiff	$3,\!145,\!868$	$2,\!860,\!031$	$2,\!859,\!201$	$2,\!859,\!593$	$2,\!861,\!763$	2,860,071	$2,\!859,\!441$
2.2.13.tiff	3,145,868	3,047,532	3,046,704	3,046,353	3,049,369	3,047,596	3,046,421
2.2.17.tiff	3,145,868	3,009,587	3,008,758	$3,\!008,\!537$	3,011,281	3,009,626	$3,\!008,\!494$
2.2.24.tiff	3,145,868	3,046,918	$3,\!046,\!087$	$3,\!045,\!762$	3,048,612	3,046,962	3,045,805
3.2.25.tiff	1,048,710	979,211	$979,\!121$	$979,\!305$	$979,\!442$	$979,\!256$	$979,\!329$

Table 5.5

File sizes (bytes) in arithmetic coding compression *Type_10*, *Type_11*, *Type_12*; *Type_20*, *Type_21*, *Type_22* over misc files

Name of file		0 x			0 x		0 x
4.2.03.tiff	786,572	763,514	$763,\!561$	$763,\!584$	764,368	764,342	764,323
5.1.09.tiff	$65,\!670$	$55,\!305$	$55,\!383$	$55,\!335$	$56,\!165$	56,166	$56,\!175$
5.1.14.tiff	$65,\!670$	60,504	60,563	60,524	$61,\!377$	$61,\!378$	$61,\!379$
5.3.02.tiff	1,048,710	895,816	895,895	896,269	896,646	$896,\!603$	$897,\!291$
7.1.07.tiff	262,278	$196,\!833$	197,042	$197,\!536$	$197,\!615$	$197,\!632$	$198,\!282$
boat.512.tif:	f 262,278	$236,\!053$	$236,\!191$	$236,\!425$	$236,\!898$	$236,\!895$	$236,\!936$

Table 5.6

File sizes (bytes) in arithmetic coding compression *Type_30*, *Type_31*, *Type_32*; *Type_40*, *Type_41*, *Type_42* over misc files

Name of file a	& its size	$Type_30$	$Type_31$	$Type_32$	$Type_40$	$Type_41$	$Type_42$
4.2.03.tiff	786,572	777,736	777,686	777,740	$777,\!886$	777,783	777,770
5.1.09.tiff	$65,\!670$	60,748	60,750	60,772	60,799	60,799	60,813
5.1.14.tiff	$65,\!670$	$63,\!514$	$63,\!515$	$63,\!525$	$63,\!565$	$63,\!564$	$63,\!572$
5.3.02.tiff	1,048,710	980,077	$979,\!98$	980,122	980,309	980,122	980,218
7.1.07.tiff	262,278	239,514	239,511	239,593	239,573	239,562	$239,\!615$
boat.512.tiff	262,278	248,767	248,764	$248,\!879$	$248,\!827$	$248,\!815$	$248,\!867$

quency table which is 1024 bytes long (byte input symbol). The compressed files shown on Table 5.6 (second part) include appropriate frequency table which is 64 bytes long (nibble input symbol). Accordingly to the results of arithmetic compression shown in the tables for our set of test files we can choose $Type_10$ (an input symbol is a byte, we use adaptive model with non-scaled frequency table) as suitable method in our set of 12 types of arithmetic compression.

At last we decompressed all our compressed files to test our application and the UPN models which refer to arithmetic decompression.

6 Conclusion

An Upgraded Petri nets are suitable for modeling various types of arithmetic coding at any level. Original software for modeling and simulations of Upgraded Petri net, PeM (Petri Net Manager), is developed and used for all models described in this paper. Several UPN models are shown. These models represent arithmetic coding from general level of representation up to register level of representation. By executing of given UPN models of an arithmetic coding the models pass through many states which are the states of arithmetic coding algorithm. After careful analysis of the models we transform these models into the real application. By using this application and PeM we do several cycles modeling-simulation-analysis and finally check suitability of given UPN models. After that we use our twelve types of arithmetic coding over the set of test images. These types are determined by input parameters: symbol type, adaptive or static data set and scale frequency table type. Finally, we represent results of all of these types of arithmetic coding over the sets of some test images (textures, aerial, misc). All models are observed in the experiments by using created application over standard set of files. Experimental results are presented and compared.

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References

- Rung-Ching Chen, Pei-Yan Pai, Yung-Kuan Chan, Chin-Chen Chang, Lossless image compression based on multiple-tables arithmetic coding, Mathematical Problems in Engineering, Vol. 2009, Article ID 128317, (2009), 13 pages, doi:10.1155/2009/128317.
- [2] D. Gašević, V. Devedžić, *Teaching Petri Nets Using P3*, IEEE Educational Technology & Society, Vol. 7, No. 4 (2004), pp. 153–166.

- [3] M. Grangetto, E. Magli, G. Olmo, Distributed arithmetic coding, IEEE Commun. Lett., Vol. 11, no. 11 (2007), pp. 883–885.
- M. Grangetto, E. Magli, G. Olmo, Rate-compatible distributed arithmetic coding, IEEE Commun. Lett., Vol. 12, no. 8 (2008), pp. 575–577.
- [5] M. Guazzo, A general minimum-redundancy source-coding algorithm, IEEE Trans. Information Theory, IT-26 (1) (1980), pp. 15–25.
- [6] P.G. Howard, J.S. Witter, Arithmetic coding for data compression, Proceedings of IEEE, Vol. 82, No. 6 (1994), pp. 857–865.
- [7] H. Kim, J. Wen, J.D. Villasenor, Secure arithmetic coding, IEEE Trans. Signal Processing, Vol. 55, No. 5 (2007), pp. 2263–2272.
- [8] G.G. Langdon, Jr., An introduction to arithmetic coding, IBM J. Res. Develop., Vol. 28, No. 2 (1984), pp. 135–149.
- [9] D.J.C. MacKay, Information Theory, Inference, and Learning Algorithms, Cambridge University Press, 2003.
- [10] A. Moffat, R.M. Neal, I.H. Witten, Arithmetic coding revisited, ACM Transactions on Information Systems, Vol. 16 (1998), pp. 256–294.
- [11] T. Murata, Petri Nets: Properties, Analysis and Applications, Proceedings of the IEEE, Vol. 77, No. 4 (1989), pp. 541–580.
- [12] R. Pasco, Source Coding Algorithms for Fast Data Compression, Stanford University, Ph.D. Thesis, 1976.
- [13] J.J. Rissanen, Generalized kraft inequality and arithmetic coding, IBM J. Res. Develop. (1976), pp. 198–203.
- [14] J.J. Rissanen & G. G. Langdon, Arithmetic coding, IBM J. Res. Develop. (1979), pp. 146–162.
- [15] F. Rubin, Arithmetic stream coding using fixed precision registers, IEEE Trans. Information Theory, IT-25 (6) (1979), pp. 672–675.
- [16] A. Said, Introduction to Arithmetic Coding Theory and Practice, Imaging Systems Laboratory HP Laboratories Palo Alto HPL-2004-76, 2004.
- [17] P. S. Strbac, An Approach to Modeling Communication Pprotocol by Using Upgraded Petri Nets, PhD Dissertation, Military Academy, Belgrade, Serbia, 2002.
- [18] I.H. Witten, R.M. Neal, J.G. Cleary, Arithmetic coding for data compression, Communications of the ACM, Vol. 30 (1987), pp. 520–540.
- [19] B. Zhu, E. Yang, A.H. Tewfik, Arithmetic coding with dual symbol sets and its performance analysis, IEEE Transactions on Image Processiong, Vol. 8, No. 12 (1999), pp. 1667–1676.
- [20] The USC-SIPI Image Database, University of Southern California: http://sipi.usc.edu/database/