



70 година рада Математичког института САНУ

ПРОГРАМ

Минисимпозијум

**„Нелинеарне теоријске основе
у опису појава реалног света“**

Пројекат ON174001 у Математичком институту САНУ,
Београд, 30 новембар 2016

PROGRAM

Mini-Symposium

**“Non-Linear theoretical basis
in description of real world phenomena“**

Project ON174001 in Mathematical Institute SASA,
Belgrade, November 30, 2016

Organizers:

dr Julijana Simonović,

Faculty of Mechanical Engineering,
University of Niš, Serbia



70 years of the Mathematical Institute of SASA, Belgrade, Serbia

Mini-Symposium

“Non-Linear theoretical basis in description of real world phenomena“

Project ON 174001 in Mathematical Institute of SASA, Belgrade, Serbia, November 30, 2016

Acknowledgment: The Mini-Symposium “Non-Linear theoretical basis in description of real world phenomena” has been organized by Project **ON 174001** in the scope of the 70th anniversary of the Mathematical Institute of the Serbian Academy of Science and Arts. The Mini-Symposium was organized thanks to the financial support from the Serbian Ministry of Education, Science and Technological Development under the project:

ON 174001 “Dynamics of hybrid systems with complex structures. Mechanics of Materials”, coordinated through Mathematical Institute of Serbian Academy of Sciences and Arts with Project Leader **Katica (Stevanović) HEDRIH**.

A WORD FROM THE ORGANIZER

*“As far as the laws of mathematics refer to reality,
they are not certain, and as far as they are certain,
they do not refer to reality.”*

A. Einstein

The concept of linear relationship suggests that two quantities are proportional to each other: doubling one causes the other to double as well. Nonlinear relationships, in general, are any relationship which is not linear. What is important in considering nonlinear relationships is that a wider range of possible dependencies is allowed. When there is very little information to determine what the relationship is, assuming a linear relationship is simplest and thus, by Occam's razor, is a reasonable starting point. However, additional information generally reveals the need to use a nonlinear representation on the description of real world phenomena.

One of the most important modern theoretical developments has been the qualitative theory of differential equations, otherwise known as dynamical systems theory, which seeks to establish general properties of solutions from general principles without writing down any explicit solutions at all. Dynamical systems theory combines local analytic information, collected in small “neighbourhoods” around points of special interest, with global geometric and topological properties of the shape and structure of the manifold in which all the possible solutions, or paths, reside—the qualitative aspect of the theory. (A manifold, also known as the state space or phase space, is the multidimensional analog of a curved surface.) The qualitative theory of differential equations was the brainchild of the French mathematician Henri Poincaré at the end of the 19th century. Today the term chaos is used to refer to Poincaré's discovery while solving the “three-body problem”. Sporadically during the 1930s and '40s and with increasing frequency in the 1960s, mathematicians and scientists began to notice that simple differential equations can sometimes possess extremely complex solutions. The American mathematician Stephen Smale, continuing to develop Poincaré's insights on qualitative properties of differential equations, proved



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that in some cases the behaviour of the solutions is effectively random. Even when there is no hint of randomness in the equations, there can be genuine elements of randomness in the solutions. The Russian school of dynamicists under A. Kolmogorov, V. Arnold, A. Andronov, A. Vitt and S. Haykin developed similar ideas at much the same time. Later I.M. Babakov and A. Lyapunov with his theory of stability and A. Krylov, N. Bogolyubov and Y. Mitropolyski with their asymptotic method designed the directions for practical application of nonlinear theory. By the end of the 20th century, Poincaré's discovery of chaos had grown into a major discipline within mathematics, connecting with many areas of applied science. Chaos was found not just in the motion of the planets but in weather, disease epidemics, ecology, fluid flow, electrochemistry, acoustics, even quantum mechanics. The most important feature of the new viewpoint on dynamics—popularly known as chaos theory but really just a sub-discipline of dynamical systems theory—is not the realization that many processes are unpredictable. Rather, it is the development of a whole series of novel techniques for extracting useful information from apparently random behaviour.

Among the Serbian schools of nonlinear mechanics, that starts with peonier M. Petrovic the Poincaré's student, it is worth to outline the one that have been begun with ideas of D. Raskovic which have been followed by the group of researchers with whole series of research in the field of nonlinear oscilations of deformabile bodies at Mechanical Faculty University of Nis. Starting with 1991 this group has been organized series of Mini-symposiums of nonlinear mechanics; this very Mini-symposium belongs to that serie and to this ideas.

Nonlinear theoretical basis, here encompassed, have led to the discovery of new and more efficient ways to present, examine and explaine: classes of vibro-impact systems dynamics, mechanical systems with nonlinear nonholonomic constraints, dynamics reanalysis procedures, dynamic behavior of cable net roofs, dynamic of composite laminates, flow around bluff bodies as well as response of robotic system, or to solve mathematical complexities as Lie group settings. It has even been turned into a better description of neuronal systems behavior or of moleculs of Zona Pelucida dynamics.

It was unexpected accolade and extremely honored to me have been given such an opportunity for organization of this kind of event.

dr Julijana Simonović

РЕЧ ОРГАНИЗАТОРА

*“Све док закони математике описују стварност они нису
поуздани, а ако су поуздани они не описују стварност“*

А. Анштајн

Концепт линеарне везе два квантитета значи да су пропорционални један другоме: удвострчавање једног изазива удвостучавање и другог. Нелинеарна веза, уопштено, је било која веза која није линеарна. Оно битно у нелинеарном приступу је ширина опсега могућих зависности које су дозвољене. Када имамо на располагању мало информација да би одрадили какав је однос, претпоставља се да је линеарни однос најједноставнији, а тиме, према окамитој оштрици, и најразумнија полазна тачка. Ипак, додатне информације откривају потребу да се употребе нелинеарне везе у опису појава реалног света.

Један од најбитнијих развоја модерних теорија примењене математике је квалитативна теорија диференцијалних једначина, иначе позната као теорија динамичких система, која развија општа својства решења из општих принципа без извођења тачног решења. Теорија динамичких система комбинује информације локалних аналитичких особина, издвојених из понашања решења у блиској околини тачака од посебног интереса, са глобалним геометријским и тополошким особинама облика и структуре вишеструкости у којој се појављују сва могућа решења-што су квалитативни аспекти теорије (Вишеструкости, такође познате и као простор стања или фазни простор, су вишедимензионалне аналогije закривљених површина). Квалитативна теорија диференцијалних једначина је замисао француског математичара Х. Пуанкареа са краја 19. столећа. Данас се израз хаос користи да се опише Пуанкареово решење „проблема три тела“. Спорадично током тридесетих и четрдесетих година прошлог века са растућом фреквенцијом од 1960, научници и математичари су почели примећивати да једноставне диференцијалне једначине могу понекад имати јако компликована решења. Амерички математичар С. Смајл, настављајући да развија Пуанкареова открића квалитативних особина диференцијалних једначина, проналази да је у неким случајевима понашање решења изузетно неочекивано (случајно). Чак и када нема ни наговештаја случајности у једначини, може да постоји оригинални елемент случајности у решењу. Руска школа механичара предвођени А. Колмогоровом, В. Арнолдом, А. Витом и С. Хајкеном развијају сличне идеје скоро у исто време. Касније И.М. Бабаков и А. Љапунов са својом

теоријом стабилности као и А. Крилов, Н. Богољубов и Ј. А. Митропољски са њиховом асимптотском методом одређују правце практичних примена нелинеарне теорије динамичких система. Тако је до краја двадесетог столећа, Поенкареово откриће хаоса прерасло у главну дисциплину у области математике, повезујући је са многим областима примењених наука. Хаос је пронађен не само у кретању планета него и у променама временских прилика, епидемијама болести, екологији, струјању флуида, електрохемији, акустици, чак и у квантној механици. Најбитније својство новог становишта динамике-популарно названо теорија хаоса али заправо је само под-дисциплина теорије динамичких система-није третирање система као непредвидивих. Заправо је то развој читаве серије нових техника за издвајање корисних информација из наизглед случајног понашања.

Међу школама нелинеарне механике у Србији, које почињу са пиониром М. Петровићем Поенкареовим студентом докторантом, вредно је поменути ону која је почела са идејама Д. Рашковића, од 1967, праћена групом истраживача са читавом серијом истраживања у области нелинеарних осцилација деформабилних тела на Машинском факултету у Нишу. Почевши од 1991. год. ова група организује серије симпозијума и мини симпозијума нелинеарне механике; Мини симпозијум који се сада организује припада том низу и идејама.

Нелинеарне теоријске основе, овде обухваћене, довеле су до открића нових и ефикаснијих начина да се представе, проуче и објасне: класе динамике виброударних система, механичких система са нехомномним нелинеарним везама, процедуре динамичке реанализе, динамичко понашање кровова од мрежа каблова, динамика композитних ламината, опструјавање неаеродинамичких тела као и одговори роботских система, или да се реше математичке сложености као што су Лие групе. Чак су боље описана и објашњена понашања неуронских система као и динамика молекула Зоне Телуциде.

Ово је неочекивано признање и изузетна почаст да ми се пружи могућност организације оваквог научног скупа.

др Јулијана Симоновић



70 years of the Mathematical Institute of SASA, Belgrade, Serbia

Mini-Symposium

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Project ON 174001 in Mathematical Institute of SASA, Belgrade, Serbia, November 30, 2016

PROGRAM

MINI-SYMPOSIUM

“Non-Linear theoretical basis in description of real world phenomena“

Project OI174001 in Mathematical Institute of SASA

Belgrade, Serbia, November 30, 2016, from 10:30-20:00h, room II, first floor, Kneza Mihaila 36

Програм

Мини-симпозијума

„Нелинеарне теоријске основе у опису појава реалног света “

Пројекат ОИ174001 у Математичком институту САНУ

Београд, 30. новембар 2016, од 10:00-20:00h, сала II, први спрат, Кнеза Михаила 36

Organizer:

dr **Julijana Simonović**, Assistant Professor, Faculty of Mechanical Engineering, University of Niš, Serbia

Организатор:

др **Јулијана Симоновић**, доцент, Машински факултет Универзитета у Нишу, Србија

Welcome address:

Professor **Katica (Stevanović) Hedrih**, Project Leader of Project ON174001

Opening remarks by Organizer:

“Importance of Research of Non-Linear theoretical basis in description of real world phenomena“

dr **Julijana Simonović**

Поздравна реч:

Професор **Катица (Стевановић) Хедрих**, руководилац Пројекта ОН174001

Уводна реч организатора:

„Значај истраживања у области Нелинеарних теоријских основа у опису појава реалног света “

др **Јулијана Симоновић**

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First Session chair by:

Isabella Vassilopoulou, *Civil Engineer, Ph.D. School of Civil Engineering, National Technical University of Athens, Greece*

Dragan Milosavljevic, *Faculty of Engineering University of Kragujevac, Serbia*

Julijana Simonović, *Faculty of Mechanical Engineering, University of Niš, Serbia,*

First Session - Invited Lectures 30 minutes.

*** Numerical integration of rotational quaternions using non-redundant ordinary differential equations in Lie group setting**

Zdravko Terze

Faculty of Mechanical Eng. and Naval Arch., Chair of Flight Vehicle Dynamics, Head
University of Zagreb, Croatia

Нумеричка интеграција ротацијских кватерниона користећи нередундантне обичне диференцијалне једнацбе у формулацији Лијевих група

Здравко Терзе

Факултет машинства и бродоградње,
Универзитета у Загребу, Хрватска

***Methodology of the investigation of a class of the vibro-impact system dynamics**

Katica R. (Stevanović) Hedrih^{1,2}

¹*Department of Mechanics, Mathematical Institute of Serbian Academy of Sciences and Arts, Belgrade, Serbia*

²*Faculty of Mechanical Engineering, University of Niš, Serbia, E-mail: khedrih@sbb.rs*

Методологија истраживања једне класе динамике вибро-ударних система

Катица Р. (Стевановић) Хедрих^{1,2}

¹*Одељење за механику, Математички институт САНУ, Београд, Србија, E-mail: khedrih@sbb.rs*

²*Машински факултет Универзитета у Нишу, Србија, E-mail: katica@masfak.ni.ac.rs*

***Dynamics of Mechanical Systems with Nonlinear Nonholonomic Constraints-Integral of Motion**

Dragomir N. Zeković

*Faculty of Mechanical Engineering, University of Belgrade
Kraljice Marije 16, 11120 Belgrade, Serbia, E-mail: dzekovic@mas.bg.ac.rs*

Динамика механичких система са нелинеарним нехолономним везама-интеграли кретања

Драгомир Н. Зековић

*Машински факултет, Универзитет у Београду,
Краљице Марије 16, 11120 Београд, Србија,
E-mail: dzekovic@mas.bg.ac.rs*



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Second Session chair by:

Zdravko Terze, Faculty of Mechanical Eng. and Naval Arch., Chair of Flight Vehicle Dynamics, Head
University of Zagreb

Dragomir N. Zeković, Faculty of Mechanical Engineering, University of Belgrade

Katica R. (Stevanović) Hedrih, Department of Mechanics, Mathematical Institute of SASA, Belgrade and
Faculty of Mechanical Engineering, University of Niš, Serbia

Second Session. Invited Lectures 30 minutes.

*** Exploring nonlinearities in the dynamic behavior of cable net roofs**

Isabella Vassilopoulou

Civil Engineer, Ph.D. School of Civil Engineering
National Technical University of Athens, Greece

E-mail: isabella@central.ntua.gr

Истраживање нелинеарности у динамици кровова мрежа каблова

Isabella Vassilopoulou

Грађевинска школа Националног Техничког Универзитета у Атини, Грчка

E-mail: isabella@central.ntua.gr

***Uncertainty Quantification and Simulation in Dynamics Reanalysis Procedures**

Nataša Trišović and Wei Li

Faculty of Mechanical Engineering, University of Belgrade, E-mail: ntrisovic@mas.bg.ac.rs and
School of Mathematics and Statistics, Xidian University, Xi'an China

E-mail: liweilw@mail.xidian.edu.cn

**Квалификација и симулација неизвесности у процесу
динамичке реанализе конструкција**

Наташа Тришовић и Wei Li

Машињски факултет, Универзитета у Београду, E-mail: ntrisovic@mas.bg.ac.rs и

Школа Математике и статистике, Xidian Универзитет, Xi'an Кина

E-mail: liweilw@mail.xidian.edu.cn

***Multiparametric nonlinear dance of synchronization in system of
orthogonal lattice of chained material particles**

Julijana Simonović

Faculty of Mechanical Engineering, University of Niš, Serbia,

E-mail: simonovicjulijana@gmail.com

**Вишепараметарски нелинеарни плес синхронизације у систему
ортогоналне решетке ланца материјалних тачака**

Julijana Simonović

Машињски факултет Универзитета у Нишу, Србија,

E-mail: simonovicjulijana@gmail.com



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KOKTEJL - СОСТАЈЛ (approximately from 14:15-15:15h)

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Third Session chair by:

Nataša Trišović, *Faculty of Mechanical Engineering, University of Belgrade, Serbia*

Jasmina Bogdanović-Jovanović, *Faculty of Mechanical Engineering University of Niš, Serbia*

Milan Cajić, *Mathematical Institute of the SASA Belgrade, Serbia*

Third Session. Invited Lectures 30 minutes.

*** Dynamic behavior of composite laminates**

Dragan Milosavljević

Faculty of Engineering University of Kragujevac, Kragujevac, Serbia

E-mail: dmilos@kg.ac.rs

Динамичко понашање композитних ламината

Драган Милосављевић

Факултет инжењерских наука Универзитет у Крагујевцу, Крагујевац, Србија

E-mail: dmilos@kg.ac.rs

***Nonlinear theoretical basis in the description of
the behavior of neuronal systems**

Ines Grozdanović

Faculty of Mining and geology University of Belgrade, Serbia

E-mail: ines.grozdanovic@rgf.bg.ac.rs

**Нелинеарне теоријске основе у опису
понашања неуронских система**

Инес Гроздановић

Рударско геолошки факултет Универзитета у Београду, Србија

E-mail: ines.grozdanovic@rgf.bg.ac.rs

Fourth Session chair by:

Ines Grozdanović, Faculty of Mining and geology University of Belgrade, Serbia

Jasmina Bogdanović-Jovanović, Faculty of Mechanical Engineering University of Niš, Serbia

Andjelka Hedrih, Mathematical Institute SASA

Fourth Session, Part One - Invited Lectures 30 minutes

*** Flow around bluff bodies- experimental and numerical investigations**

Jasmina Bogdanović-Jovanović

Faculty of Mechanical Engineering University of Niš, Serbia

E-mail: bminja@masfak.ni.ac.rs

**Опструјавање тупих тела (неаеродинамичког облика) –
експериментална и нумеричка истраживања**

Јасмина Богдановић-Јовановић

Машински факултет Универзитет у Нишу, Србија

E-mail: bminja@masfak.ni.ac.rs

*** Response of a three degree of freedom robotic system
with fractional order elements**

Milan Cajić

Mathematical Institute of the SASA, University of Belgrade, Serbia

E-mail: mcajic@mi.sanu.ac.rs

**Одзив роботског система са три степена слободне кретања и
везаним елементима фракционог реда**

Милан Цајић

Математички институт САНУ, Универзитет у Београду, Србија

E-mail: mcajic@mi.sanu.ac.rs

***Non-linear dependens of stress and deformation tensor elements and
specific deformation work in linearized quazi static model of Zone Pelucida**

Andjelka Hedrih¹, Katica (Stevanovic) Hedrih^{1,2}

¹Department of Mechanics, Mathematical Institute of Serbian Academy of Sciences and Arts,
Belgrade, Serbia, E-mail: handjelka@hm.co.rs ,

²Faculty of Mechanical Engineering, University of Niš, Serbia,
E-mail: katica@masfak.ni.ac.rs

**Нелинеарност промене елемената тензора напона, тензора деформације и
и специфичног деформационог рада у линеаризованом квазистатилком
моделу Зоне пелуциде**

Анђелка Хедрих¹, Катица (Стевановић) Хедрих^{1,2}

¹Одељење за механику, Математички институт САНУ, Београд, Србија,
E-mail: handjelka@hm.co.rs ,

²Машински факултет, Универзитета у Нишу, Србија,
E-mail: katica@masfak.ni.ac.rs



dr Julijana Simonović, Mech. Eng.,

Assistant Professor Mechanical Faculty University of Nis, Serbia

Date of birth: Avg.1975

Address: Bulevar Nikole Tesle 55/16, Nis, Serbia

Tel. at work: +381-18-500-725

Mobile: +381-62-260-190

Emails: bjulijana@masfak.ni.ac.rs, simonovicjulijana@gmail.com

Work experience: Feb. 2001 – Nov. 2016: Teaching Assistant in the field of Mechanics (subjects: Elastodynamics, Mechanics III-Dynamics, Mechanics II-Kinematics, Mechanics I-Static and Straight of materials) Department of Mechanics, Mechanical faculty University of Nis, Serbia

Researching Projects: Jan. 2012–Dec 2016: Researcher on Project OI174001- Dynamics of hybrid systems with complex structures. Mechanics of materials, project leader: [Dr. Katica Hedrih](#), supported by the Ministry of Sciences and Environmental Protection of Republic of Serbia through Mathematical Institute SASA, Belgrade;

Jan. 2007-Dec. 2011: Researcher on Project No 144002- Theoretical and Applied Mechanics of the Rigid and Solid Bodies. Mechanics of Materials. Supported by the Ministry of Science, Technology and Development, Serbia, project leader: Prof.dr Katica (Stevanovic) Hedrih.

Jan. 2002 – Dec. 2006: Researcher on two Projects :No 1616-Real Problems of Mechanics, Mathematical Institute SASA, No 1828-Dynamics and Control of Active Constructions, University of Nis Mechanical faculty, both supported by Ministry of Science and Protected of Leaving Environment, Serbia, both leading by Prof .dr Katica (Stevanovic) Hedrih.

Education: Dec. 2015 - Jun. 2016: post PhD research period at Interdisciplinary Centre for Mathematical and Computational Modelling of Warsaw University on subject of Bone Tissue Advanced Modeling with Piezoelectricity. Supported by the ERASMUS MUNDUS ACTION 2 PROJECT SIGMA AGILE.

Dec 2012: public defense of doctoral dissertation: „*Dynamics and Stability of Dynamics Hybrid Systems*“, mentored by Prof.dr Katica (Stevanović) Hedrih

Sep. 2009: participant of CF SICON Event: Nonlinear Dynamics, Stability, Identification and Control of Systems and Structures at La Sapienza University of Rome.

April 2009: participant of TC4 SICON event: Advanced Nonlinear Dynamics and Chaotic Dynamical Systems, ENTPE Lyon, France.

May 2008: public defense of master thesis „*Dynamics of Mechanical Systems of Complex Structure*“, mentored by Prof.dr Katica (Stevanović) Hedrih

July 2007: participant of TC1 SICON event: Stability and Bifurcations of Nonlinear Dynamical Systems, DISAT - University of L'Aquila.

2001 – 2007: Study postgraduate on Theoretical and Applied Mechanics- 4 years study program, Department of Mechanics, with two years of absence because of brings forth two children. University of Nis Mechanical faculty, Serbia.

1994 – 2000: Graduate Mechanical Engineer (Dipl. Ing) -10 semester study program, average mark 9,38 of 10.00, Department of Hydro Engineering, University of Nis Mechanical faculty, Serbia.

1982 – 1994: Primary and Grammar School, Sarajevo, Bosnia and Herzegovina, and Nis, Serbia.

IT skills: Computer literate in MS Office, MatCad, Maple, Mathematica, AnSys.

Language skills: Serbian, English (advanced), French (understand and write), German (basic)

Others: Married and mother of three children in excellent health with strong and persistent work motivation. Many different hobbies: cycling, running, yoga, swimming, reading and cooking especially kneading.

Few selected references:

1. Hedrih (Stevanović) K R. and *Simonović J.*, (2015), *Structural analogies on systems of deformable bodies coupled with non-linear layers*, Int. J. Non-Linear Mech, Volume 73, July 2015, Pages 18–24.
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ФОТО ГАЛЕРИЈА

Међународни минисимпозијум „Механика лома и нумеричке методе“
Пројекат ON174001, Београд, 16 новембар 2016

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Project ON174001, Belgrade, November 16, 2016

http://www.mi.sanu.ac.rs/novi_sajt/research/projects/174001a.php

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Ljubica Milović, Faculty of Technology and Metallurgy, University of Belgrade, Serbia





Preface



This Special Issue of IJNM, *A Phenomenological Conspectus on Nonlinear Dynamics*, emphasizes the notion that various and different physical phenomena can often be described by identical or similar mathematical instruments. In this regard, papers from disparate fields have been compiled in the issue.

It is noted that the concepts of Mathematical Phenomenology and Phenomenological Mappings are captured in the works of Professor Mihailo Petrović (1868–1943), a Serbian mathematician who was one of the doctoral students of Jules Henri Poincaré (1854–1912). The specific title of his book in French is *Mecanismes communs aux phénomènes disparates*, Paris 1921. In this book, Petrović studied (among others) certain elements of multi-dimensional geometry, couplings between mechanisms and manifestations of phenomena, quantitative vis-à-vis qualitative images of appearances (phenomena), as well as different kinds of analogies.

It is hoped that this Special Issue comprising papers of different thematic foci will serve to highlight the role of a “phenomenological” perspective for pedagogical and investigative purposes in the field of nonlinear dynamics in physically disparate systems.

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Preface

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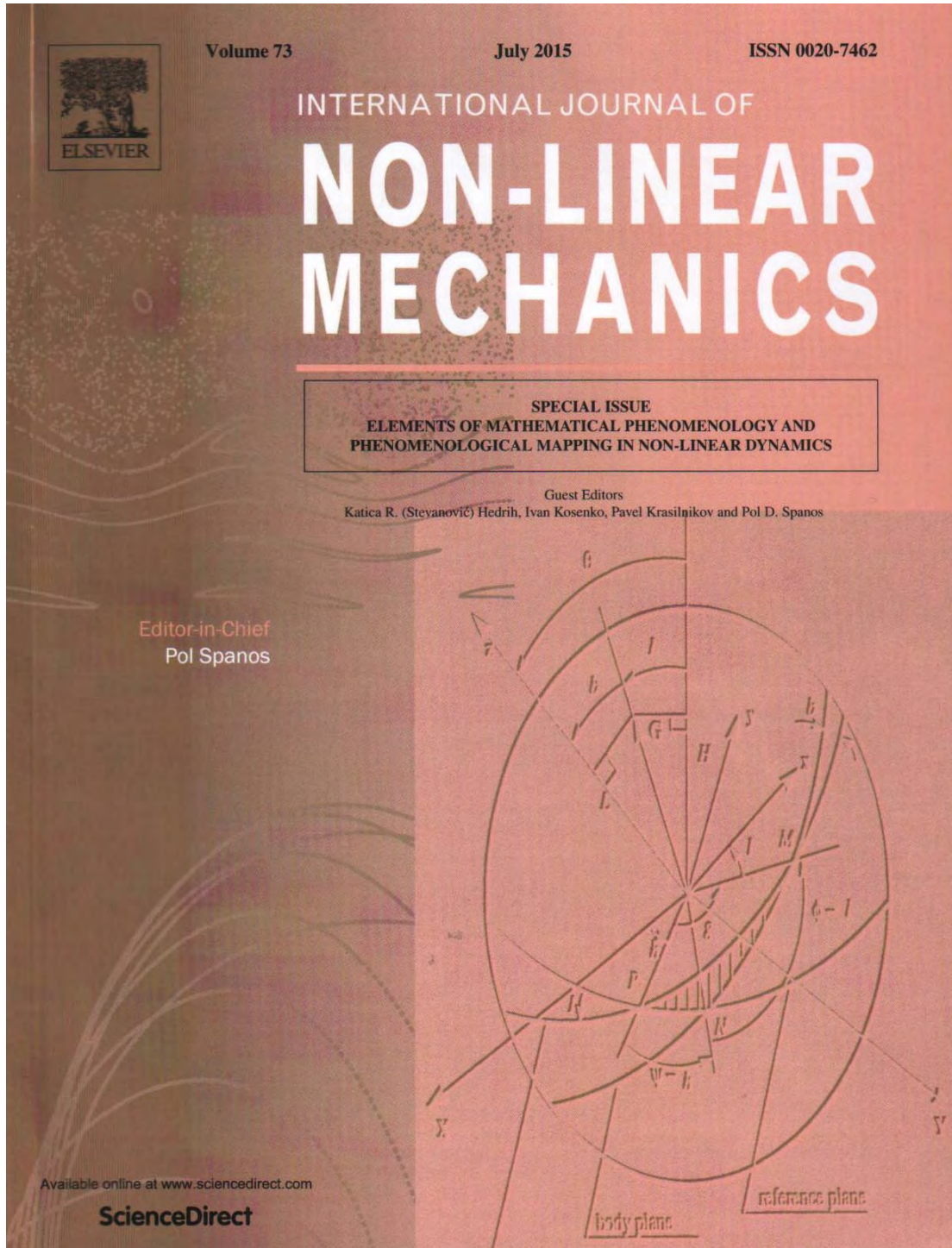


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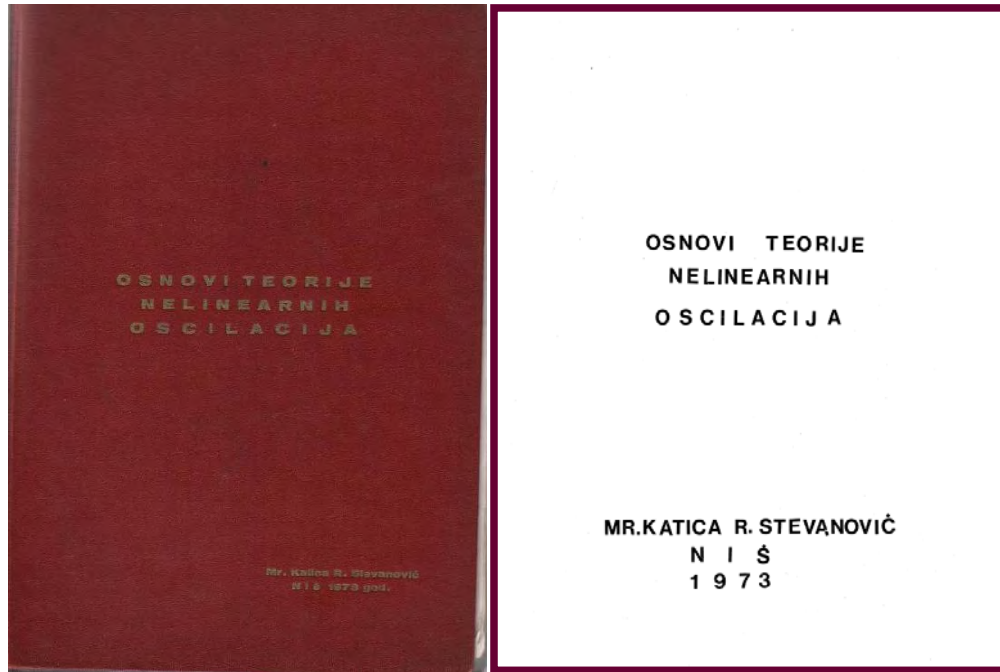
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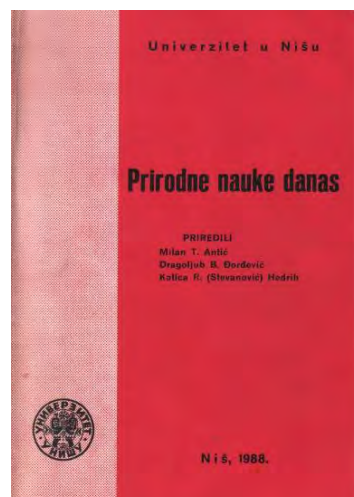
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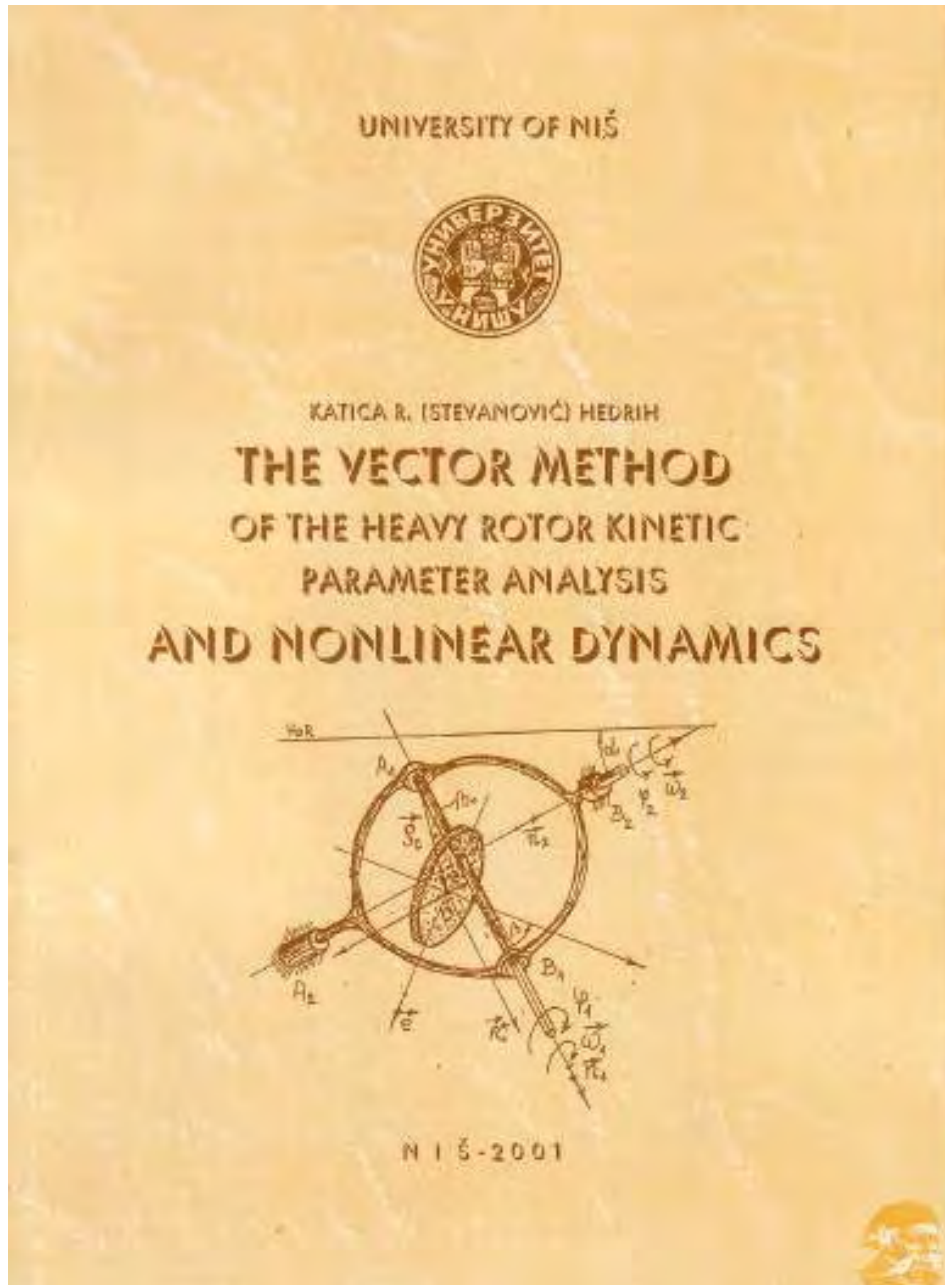
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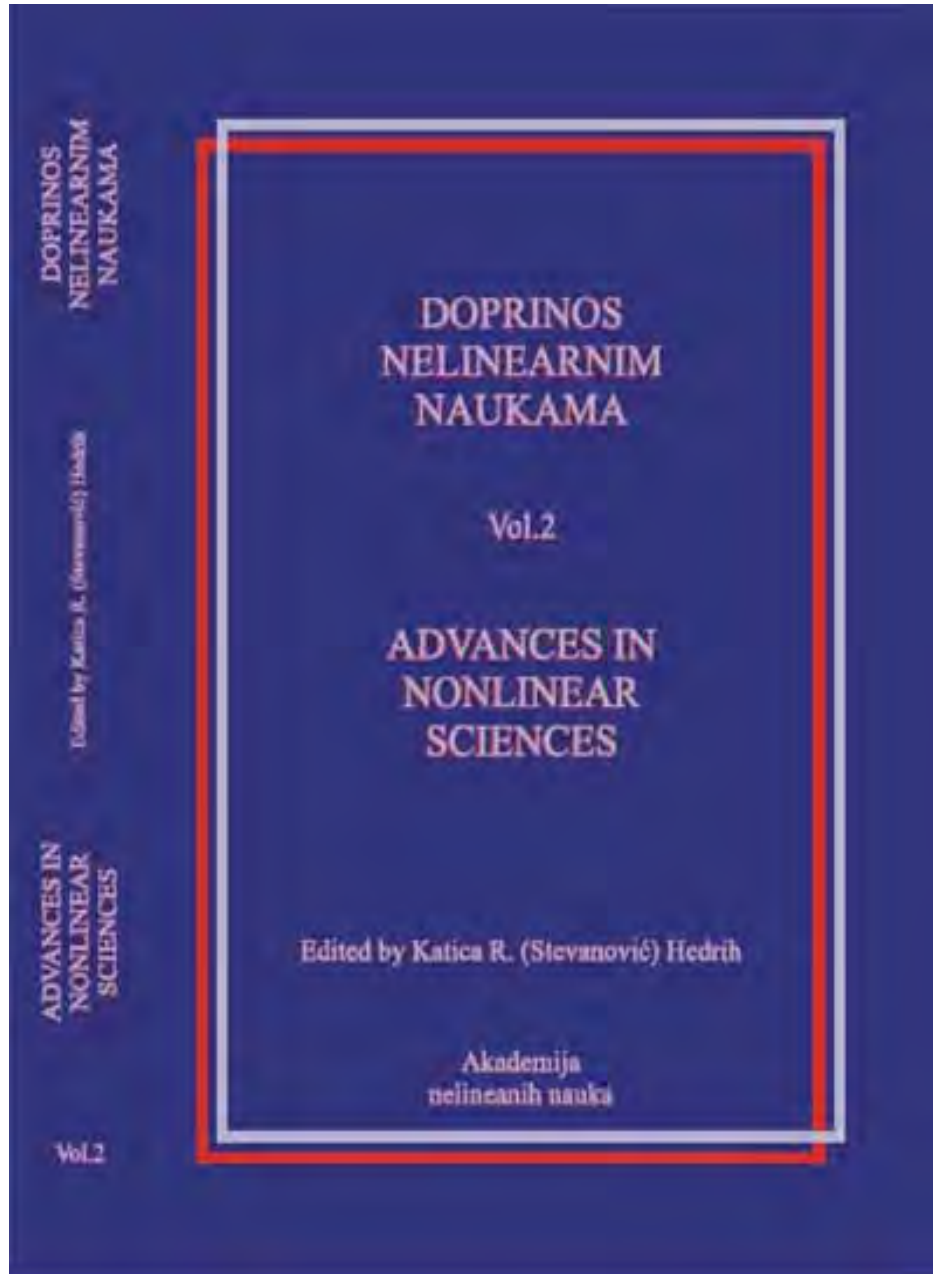


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 $\ddot{\varphi} + \Omega^2 (1 - \lambda^2) \varphi = \frac{\lambda \text{ctg} \alpha}{\sqrt{1 - \lambda^2}} \cos \Omega t$

$E_p = mgh = mg\ell [\sin \alpha (1 - \cos \varphi) - \sin \varphi \cos \alpha \cos \theta]$
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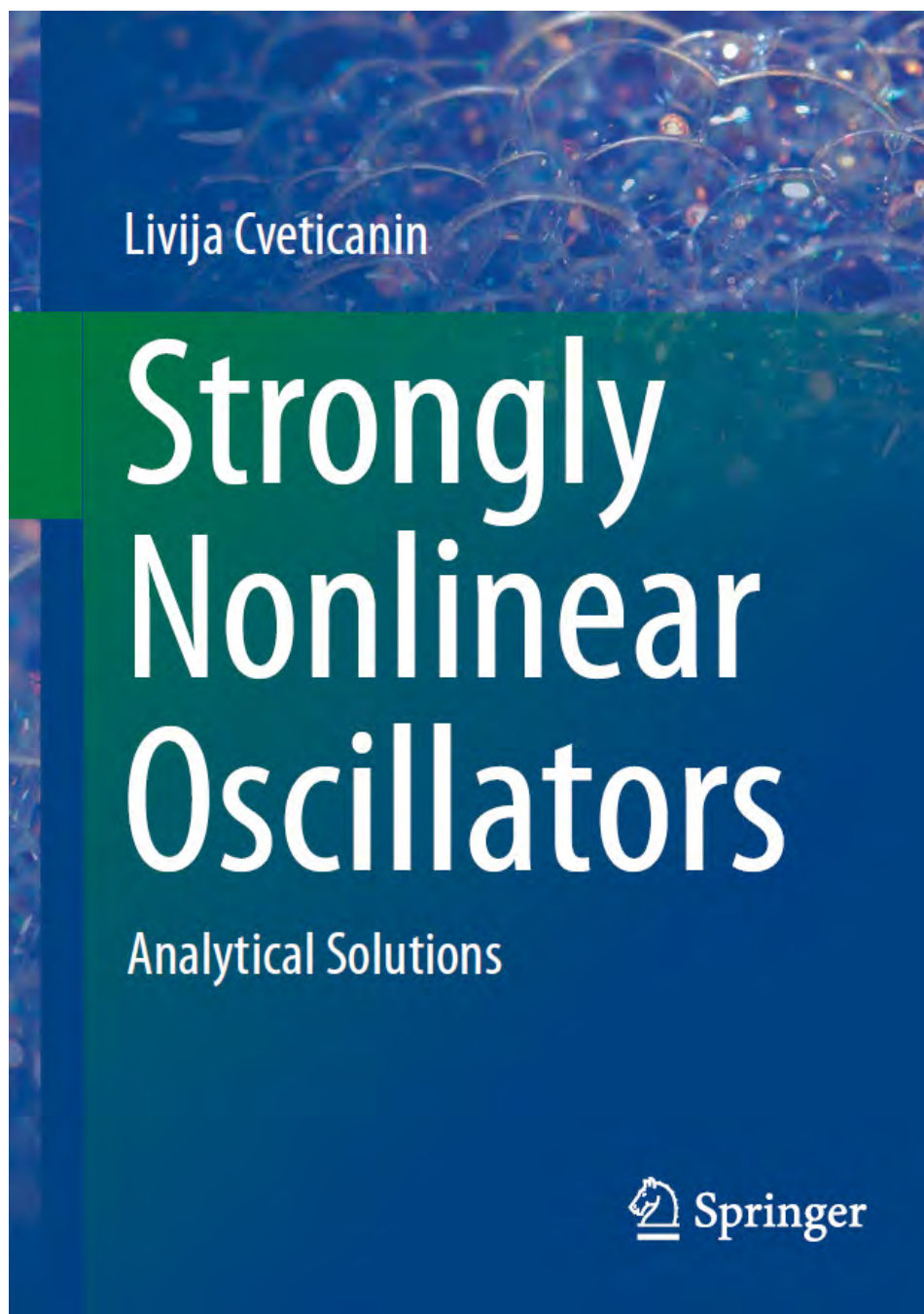


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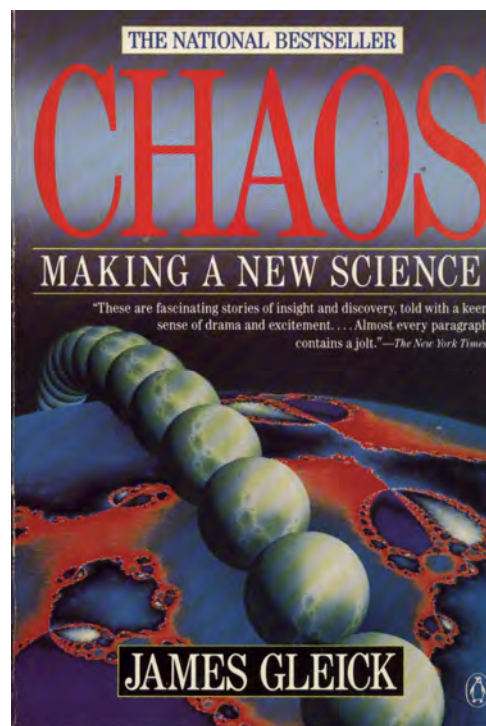
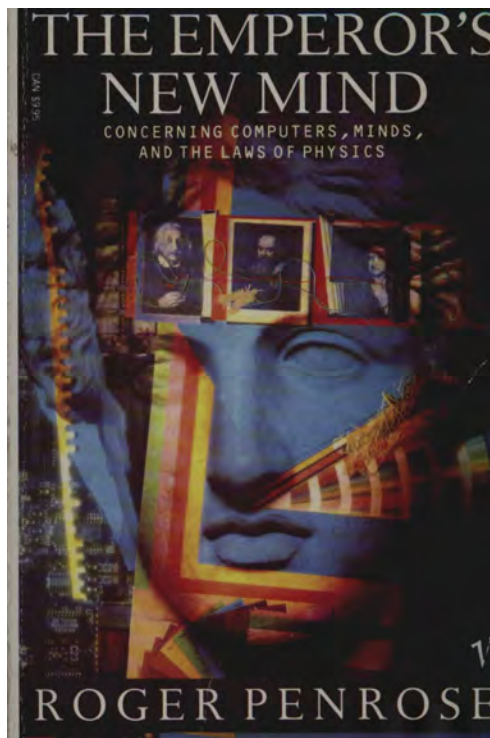
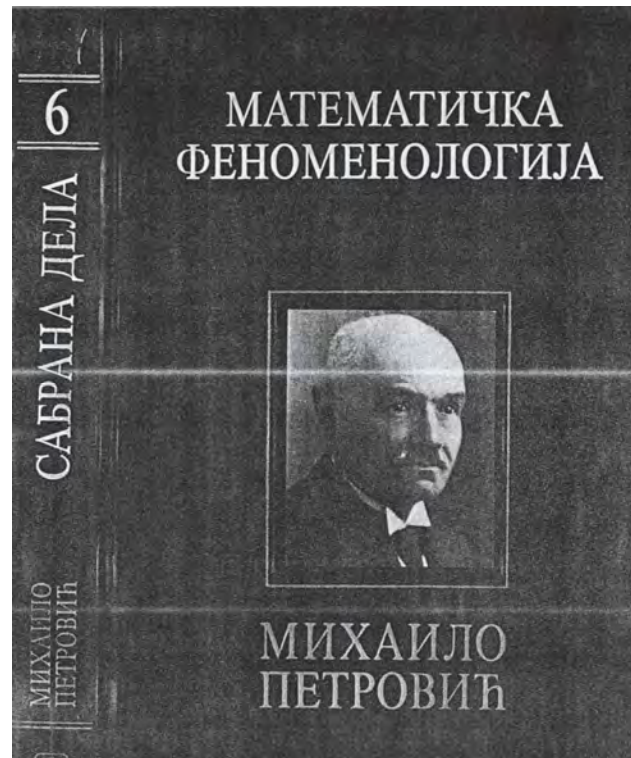
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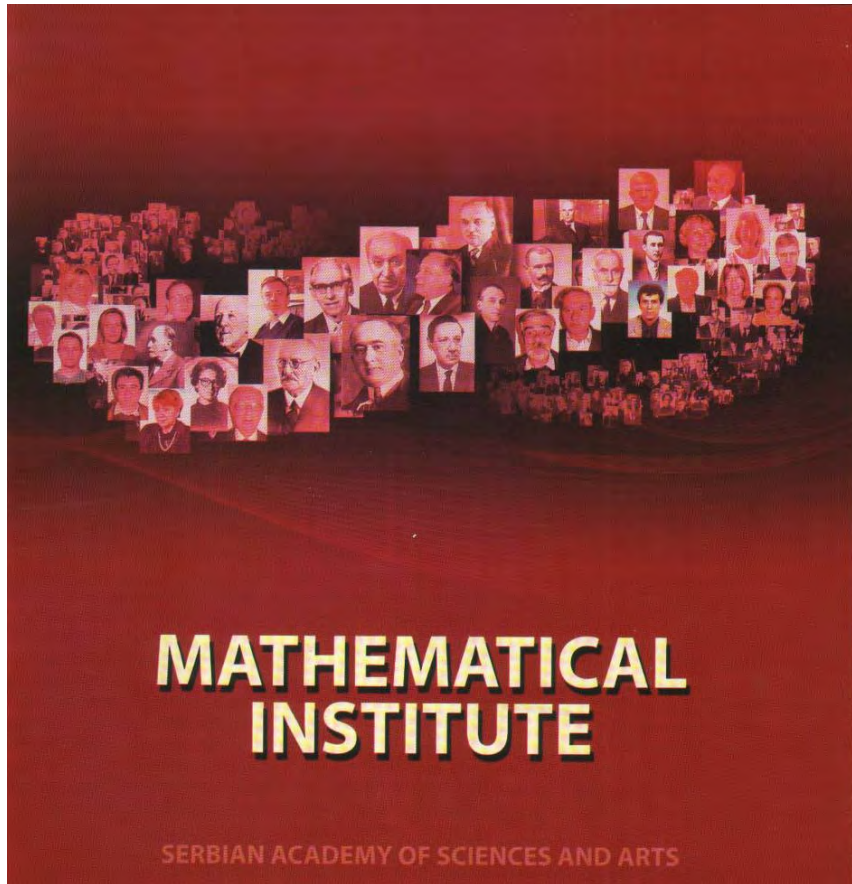


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