## THERMODYNAMICS OF BLACK HOLES: HAWKING-PAGE TEMPERATURES AND SECOND ORDER PHASE TRANSITIONS

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## ABSTRACT

In general relativity, volume is a coordinate-dependent quantity, and as a result, it is typically not included as a thermodynamic variable in the description of **black hole thermodynamics**. My presentation explores how different volume definitions can be consistently incorporated into these descriptions from a thermodynamic perspective. Various approaches in the literature are reviewed, their implications analyzed, and the conclusions discussed. The primary focus is on the phase structure of **Anti-de Sitter–Kerr black holes** and the **Hawking-Page phase transitions**. The goal is to examine the feasibility of integrating volume as a meaningful variable in the thermodynamic framework of different types of black holes.

KEYWORDS Black hole thermodynamics, Hawking-Page phase transition

## REFERENCES

- [1] Biró, T.S. and Czinner, V.G. and Iguchi, H. and Ván, P., Black hole horizons can hide positive heat capacity, *Physics Letters B*, vol. 782, pp. 228–231, 2018.
- [2] Hawking, S.W. and Page, D.N., Thermodynamics of black holes in Anti-de Sitter space, *Communications in Mathematical Physics*, vol. 87/4, pp. 577–588, 1983.
- [3] Spallucci, E. and Smailagic, A., Maxwell's Equal Area Law and the Hawking-Page Phase Transition, Journal of Gravity, 2013.
- [4] Dolan, B.P., Where is the PdV in the first law of black hole thermodynamics?, *Open Questions in Cosmology*, 2012.