

Директору Математичког института САНУ  
Проф. др Зорану Огњановићу  
Научном већу Математичког института САНУ  
академику Драгошу Цветковићу

## Стручни извештај о учешћу у научним скуповима у септембру 2015 године

I\*

**The 14th International Conference of Tensor Society on Differential Geometry and its Applications, and Informatics.** Held at Tsukuba University, Tsukuba, Japan, Sept. 7–12, 2015. Organized by Tensor Society (Tokyo) and University of Tsukuba for mutual Progress.  
c/o Kawaguchi Inst. of Math. Soc. Sengen 1-13-33, Tsukuba, Japan.  
E-mail: [tensor-ns@nifty.ne.jp](mailto:tensor-ns@nifty.ne.jp), [kawaguchi\\_tom@ybb.ne.jp](mailto:kawaguchi_tom@ybb.ne.jp)

President of Tensor Society, Prof., Dr. Tomoaki KAWAGUCHI, Tensor Society (Tokyo). c/o Kawaguchi Inst. of Math. Soc. Sengen 1-13-33, Tsukuba, Japan. E-mail: [tensor-ns@nifty.ne.jp](mailto:tensor-ns@nifty.ne.jp), [kawaguchi\\_tom@ybb.ne.jp](mailto:kawaguchi_tom@ybb.ne.jp)

Моје учешће у раду овог традиционалне међународне конференције диференцијалне геометрије и примена је реализовано следећим активностима:

- \* Чланством у председништву Конференције на отварању Конференције, а на предлог академика Милеве Првановић и председника Тензор друштва (Tensor Society (Tokyo)) професора Томоаки Кавагучија. Тим предлозима сам била заиста почаствована;
- \* Председавањем другом пленарном седницом Конференције;
- \* Учешћем питањима и коментарима на седницама Конференције;
- \* Чланством у Редакционом одбору часописа TENSOR Јапанског друштва Tensor Society;
- \* Одржаним 90-томинутним пленарним предавањем по позиву, под насловом:

Katica R. (Stevanović) Hedrih, **Structural, qualitative and mathematical analogies: Theorems of mechanical energy change in dynamics of discrete fractional order system and of a multi-deformable body fractional order system**, Dedicated to 80<sup>th</sup> Anniversary of Tensor Society President-Professor-Scientist Tomokai Kawaguchi's birthday, 90minutes Onvited Plenary Lecture, **The 14th International Conference of Tensor Society on Differential Geometry and its Applications, and Informatics.** Tensor Society (Tokyo) and University of Tsukuba for mutual Progress. Tsukuba, Japan, , Sept. 7–12, 2015., Abstracts, 2015, pp/ 2–3.

После одржаног предавања постављена су ми два питања, на која сам са задовољством одговорила. Кп,шчетам рад ће бити публикован у наредном броју часописа TENSOR Јапанског друштва Tensor Society. Цасопис се публикује већ 75 година!

Организација Конференције је била добра, предавања и саопштења на високом научном нивоу. На овој конференцији је било мање учесника него ранијих година, јер је због економске кризе отсуствовала група истраживача из Румуније, академика Раду Мирона.

С поштовањем,

У Београду, 25 септембра 2015.

*Katica R. (Stevanović) Hedrih*

Katica R. (Stevanović) Hedrih  
Руководилац пројекта OM174001

II\*

**THE 3rd INTERNATIONAL CONFERENCE MECHANICAL ENGINEERING IN XXI CENTURY, PROCEEDING, September 17 - 18, 2015, NIŠ**, Faculty of Mechanical Engineering University of Niš, pp.

У програму ове конференције била су заступљена три моја рада. Два рада су уврштена у регуларни део Конференције, а један је уврштен у део програма, који је посвећен животним јубилејима мојих некадашњих студената, од којих је један бранио докторску дисертацију пред комисијом чији сам члан била на почетку моје универзитетске активности. Тај програм је био под називом:

**MECHATRONICS AND CONTROL, COLLOQUIUM IN HONOUR OF THE 65TH BIRTHDAY OF PROF. NENAD D. PAVLOVIĆ AND PROF. TOMISLAV PETROVIĆ**

Сва три моја рада су публикована у Конференцијском Зборнику, рецензираних радова. Списак тих публикованих радова са библиографским подацима је у прилогу:

Katica (Stevanović) HEDRIH, Elements of Geometry, Kinematics and Dynamics of Billiards, MECHATRONICS AND CONTROL, COLLOQUIUM IN HONOUR OF THE 65TH BIRTHDAY OF PROF. NENAD D. PAVLOVIĆ AND PROF. TOMISLAV PETROVIĆ, THE 3rd INTERNATIONAL CONFERENCE MECHANICAL ENGINEERING IN XXI CENTURY, PROCEEDING, September 17 - 18, 2015, NIŠ, Faculty of Mechanical Engineering University of Niš, pp. 313-318. Hard Copy ISBN 978-86-6055-072-1 and CD.

Katica R. (STEVANOVIĆ) HEDRIH, Velocities of the Basic Vectors of a Tangent Space Of Moving Mass Particle Vector Position In Curvilinear Coordinate Systems, THEORETICAL AND APPLIED MECHANICS AND MATHEMATICS, THE 3rd INTERNATIONAL CONFERENCE MECHANICAL ENGINEERING IN XXI CENTURY, PROCEEDING, September 17 - 18, 2015, NIŠ, Faculty of Mechanical Engineering University of Niš, pp. 449-454. Hard Copy ISBN 978-86-6055-072-1 and CD.

Katica R. (STEVANOVIĆ) HEDRIH, The Fractional Order System Oscillations: Analytical Theory and Examples, THEORETICAL AND APPLIED MECHANICS AND MATHEMATICS, THE 3rd INTERNATIONAL CONFERENCE MECHANICAL ENGINEERING IN XXI CENTURY, PROCEEDING, September 17 - 18, 2015, NIŠ, Faculty of Mechanical Engineering University of Niš, pp. 455-460. Hard Copy ISBN 978-86-6055-072-1 and CD.

С поштовањем,

У Београду, 25 септембра 2015.



Katica R. (Stevanović) Hedrih  
Руководилац пројекта OM174001

III\*

**XIII КОНФЕРЕНЦИЈА  
ДИГИТАЛИЗАЦИЈА КУЛТУРНЕ БАШТИНЕ И ДИГИТАЛНА ХУМАНИСТИКА  
(национални скуп са међународним учешћем)**

Београд, 10 - 11. септембар 2015

XIII konferencija Digitalizacija kulturne bastine i digitalna humanistika, Beograd, 10. i 11. 9. 2015.

За ову конференцију пријавила смо три саопштења:

***Катица Р. (Стевановић) Хедрих,***

**1\* Татомир Анђелић, Данило Расковић и тензорски рачун у Србији**

**2\* Одељење за механику и Семинар механике Математичког института САНУ у периоду новембар  
2010-август 2011 године**

**3\* Пола века Катедре за механику Масинског факултета Универзитета у Нишу.**

Због подударности термина боравка у Јапану, послала сам Организаторима два постера са прво саопштење, и ПДФ фајл за друго саопштење уз комплетан текст за постављање у базу електронске библиотеке. Наравно све то уз извињење што лично већу учествовати.

Треће саопштење сам одложила за следећу конференцију да тада исто саопштим-.

С поштовањем,

У Београду, 25 септембра 2015.

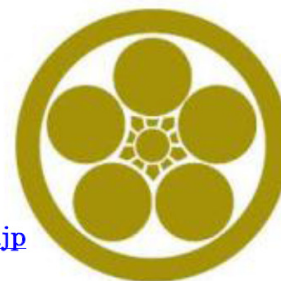
*Катица (Стевановић) Хедрих*

Katica R. (Stevanović) Hedrih  
Руководилац пројекта OM174001

# TENSOR SOCIETY

c/o Kawaguchi Institute of Mathematical Sciences  
Sengen 1-13-33, Tsukuba, 305-0047 Tsukuba, Japan  
Tel. 81-(0)29-851-5615, Fax 81-(0)29-856-6576

E-mail: [tensor-ns@nifty.ne.jp](mailto:tensor-ns@nifty.ne.jp) [kawaguchi\\_tom@ybb.ne.jp](mailto:kawaguchi_tom@ybb.ne.jp)



*President: Prof. Tomoaki KAWAGUCHI, Dr. of Eng.*

Academician, Professor, Dr. Katica R. (Stevanovi\_c) Hedrih  
Mathematical Institute Serbian Academy of Science and Arts, Belgrade  
(and Faculty of Mechanical Engineering University of Nis)  
ul. Vojvode Tankosi\_ca 3/22, 18000 Ni\_s, Serbia  
E-mail: [khedrih@eunet.rs](mailto:khedrih@eunet.rs), [katica@masfrak.ni.ac.rs](mailto:katica@masfrak.ni.ac.rs), [khedrih@sbb.rs](mailto:khedrih@sbb.rs)

Tsukuba, May11, 2015

Dear Academician, Professor, Dr. Katica R. (Stevanovic),

On behalf of Tensor Society, we would like to invite you with our great pleasure to “The 14<sup>th</sup> International Conference of Tensor Society on the Differential Geometry and its Applications, Sept. 7-12, 2015 held” at University of Tsukuba, Tsukuba, Japan, and it is very happy for us if you could present and talk some scientific activities in your special fields.

Looking forward to hearing from you concerning the above matter at your earliest convenience,

Sincerely yours

Professor, Dr. Tomoaki KAWAGUCHI

*Tomoaki Kawaguchi*

President of Tensor Society



テンゾル学会

# TENSOR

*Edited by*

**Tomoaki KAWAGUCHI**

*With the cooperation of*

S. AMARI

S. IGARASHI

R. MIRON

Y. SATO

L. TAMÁSSY

W.-G. BOSKOFF

H. KAWAGUCHI

M. PRVANOVIĆ

H. SHIMADA

K. (STEVANOVIĆ) HEDRIH

K. MATSUMOTO

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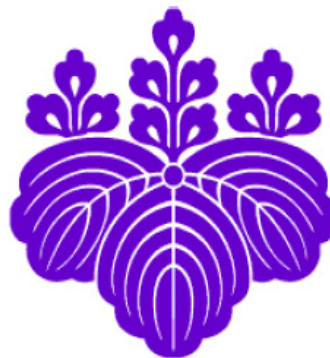
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**THE TENSOR SOCIETY**

**CHIGASAKI, JAPAN**



テンソル学会  
*Tensor Society*



筑波大学  
*University of Tsukuba*

The 14<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY  
DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS,  
AND INFORMATICS BESIDES  
— Joint Conference of Tensor Society and University of Tsukuba —  
*held at University of Tsukuba, Tsukuba, Japan, Sept. 7-12, 2015*

<The First Announcement>

Location : International conference room, University of Tsukuba

Organizing committee :

Honorary President : Shoji WATANABE (Tokyo)

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Tetsuya MIZUTANI (Tsukuba), Masaru SHIMBO (Sapporo).

The conference covers various research fields as follows :

1. Riemannian geometry and its Applications,
2. Finslerian geometry, its Applications and Higher order geometry,
3. Information geometry and its Applications,
4. Electromagnetics and Relativity,
5. Informatics,
6. Miscellaneous subject

### Participation fees :

- 1 . US \$ 200.00 for a member of Tensor Society  
( for Japanese people : ¥20,000 )
- 2 . US \$ 50.00 for an accompanied person by a member  
( for Japanese people : ¥5,000 )
- 3 . US \$ 250.00 for a non-member of Tensor Society  
( for Japanese people : ¥25,000 )
- 4 . US \$ 75.00 for an accompanied person by a non-member  
( for Japanese people : ¥7,500 )

### Accommodation and Meals :

We can offer that every foreigner and Japanese member of the society stay at University hotel at a reasonable price. The cost and its item will be notified by the second information given at the end of May, 2015.

### Correspondences:

Dr. Tomoaki KAWAGUCHI  
Tensor Society (Tsukuba)  
c/o Kawaguchi Inst.of Math.Sci.  
Sengen 1-13-33, Tsukuba, Japan  
E-mail: [tensor-ns@nifty.ne.jp](mailto:tensor-ns@nifty.ne.jp)  
Tel: 81-(0)29-851-5615 (Tsukuba)  
Fax: 81-(0)29-856-6576  
Tel/Fax: 81-(0)3-3947-3910 (Tokyo)  
Mobile: 81-090-9150-4681

Dr. Hiroaki KAWAGUCHI  
Tensor Society (Chigasaki)  
c/o Kawaguchi Inst.of Math.Sci.  
Matsu-ga-oka 2-7-15, Chigasaki, Japan  
E-mail: [tensorsociety@ybb.ne.jp](mailto:tensorsociety@ybb.ne.jp)  
Tel: 81-(0)467-83-3914 (Chigasaki)  
Fax: 81-(0)467-86-4713  
Tel/Fax: 81-(0)44-954-0427  
Mobile: 81-090-9953-9533

THE 14<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY  
Organized by Tensor Society and University of Tsukuba for mutual Progress,  
Held at Tsukuba, Japan, Sept. 7-12, 2015

PROGRAM

テンゾル学会

(TENSOR SOCIETY)



THE 14<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY

Program

September 8 (Tuesday), 2015

10:00~10:15 Opening Ceremony

Chairwoman: Prof. Mileva PRVANOVIC (Serbian Academy, Belgrade)

10:15~10:45 Lecture by Takayoshi Ootsuka.

Title: A definition of Finsler connection from the point-Finsler viewpoint.

10:45~11:15 Lecture by Takayoshi Ootsuka, Ryoko Yahagi, Muneyuki Ishida and Erico Tanaka.

Title: Energy-momentum conservation laws in Finsler / Kawaguchi Lagrangian formulation.

11:15~11:30 Coffee break.

11:30~12:00 Lecture by Erico Tanaka, Takayoshi Ootsuka, Ryoko Yahagi and Muneyuki Ishida.

Title: Relativity and Energy momentum currents by the framework of Kawaguchi geometry.

12:00~13:30 Lunch time.

Chairwoman: Prof. Katica R. (Stevanovic) HEDRIH (Serbian Academy, Belgrade)

13:30~14:00 Lecture by Tetsuya Nagano.

Title: Linear parallel displacement and the torsion tensor field P.

14:00~14:30 Lecture by Tadashi Aikou and Haripamyu.

Title: An example of Rizza-negative structures.

14:30~17:00 Free speech.

**September 9 (Wednesday), 2015**

Chairman: Prof. Koji MATSUMOTO (Yamagata)

10:00~10:30 Lecture by Masaru Shimbo, Jun Toyama and Masashi Shimbo.

Title: The Origin of the Flash Lag Illusion in the Non-Riemannian  
Multisensory  
System.

10:30~12:00 Lecture by Katica R. (Stevanovic) Hedrih.

Title: Structural, qualitative and mathematical analogies: Theorems of  
Mechanical energy change in dynamical system of discrete fractional order  
and in a multi-deformable body fractional order system.

12:00~13:30 Lunch time.

**September 10 (Thursday), 2015**

Chairman: Prof. Tadashi AIKOU (Kagoshima)

10:00~11:00 Lecture by Mileva Prvanovic.

Title: Some properties of locally decomposable Riemannian manifold and  
Kaehler manifolds of generalized quasi constant curvature.

11:00~11:30 Lecture by Koji Matsumoto

Title: Some curvaturelike Field of an almost Contact Riemannian Manifold.

11:30~13:30 Lunch time.

Chairman: Prof. Tetsuya Nagano (Nagasaki)

13:30~14:00 Lecture by Toyoko KASHIWADA

Title: A generalized Hops manifold admitting a certain symmetric property.

14:00~14:30 Lecture by Zerrin Senturk.

Title: On curvature properties of locally conformal Kaehler space forms.

14:30~15:00 Coffee break.

THE 14<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY  
Organized by Tensor Society and University of Tsukuba for mutual Progress,  
Held at Tsukuba, Japan, Sept. 7-12, 2015

ABSTRACT

テンソル学会

(TENSOR SOCIETY)

Katica R. (Stevanovic) Hedrih: Structural, qualitative and mathematical analogies: Theorems of mechanical energy change in dynamics of discrete fractional order system and of a multi-deformable body fractional order system.

(Dedicated to 80<sup>th</sup> Anniversary of Tensor Society,

2

President-Professor-Scientist Society,

*A series of theorems of mechanical energy change in dynamics of discrete fractional order system and of a multi-deformable body fractional order system are defined with corresponding proofs. Using structural, qualitative and mathematical analogies between mechanical chain system and electrical chain system the theorems of total mechanical energy change in mechanical fractional order system are presented as analogous with the theorems of total electrical energy change in electrical fractional order system.*

## **Structural, qualitative and mathematical analogies: Theorems of mechanical energy change in dynamics of discrete fractional order system and of a multi-deformable body fractional order system**

Dedicated to 80<sup>th</sup> Anniversary of  
Tensor Society President-Professor-Scientist **Tomokai Kawaguchi's** birthday

Katica R. (Stevanović) Hedrih,

Mathematical Institute SANU Belgrade, Department for Mechanics and Faculty of Mechanical Engineering, University of Niš, Serbia.  
Priv. address: 18000-Niš, ul Vojvode Tankosića 3/22, Serbia, e-mail: [khedrih@eunet.rs](mailto:khedrih@eunet.rs), [khedrih@sbb.rs](mailto:khedrih@sbb.rs).

**ABSTRACT.** A series of theorems of mechanical energy change in dynamics of discrete fractional order system and of a multi-deformable body fractional order system are defined with corresponding proofs. Using structural, qualitative and mathematical analogies between mechanical chain system and electrical chain system the theorems of total mechanical energy change in mechanical fractional order system are presented as analogous with the theorems of total electrical energy change in electrical fractional order system.

Some of theorems for discrete fractional order system dynamics are:

**Theorem 1:** For a class of fractional order non conservative system dynamic, with  $n$  degrees of freedom, and defined by: matrix of inertia properties  $\mathbf{A} = (a_{kj})_{\rightarrow j=1,2,3,\dots,n}^{\downarrow k=1,2,3,\dots,n}$ , matrix of rigidity properties  $\mathbf{C} = (c_{kj})_{\rightarrow j=1,2,3,\dots,n}^{\downarrow k=1,2,3,\dots,n}$ , matrix of viscoelastic creep fractional order properties  $\mathbf{C}_\alpha = (c_{\partial,kj})_{\rightarrow j=1,2,3,\dots,n}^{\downarrow k=1,2,3,\dots,n}$  and matrix of viscoic linear properties  $\mathbf{B} = (b_{kj})_{\rightarrow j=1,2,3,\dots,n}^{\downarrow k=1,2,3,\dots,n}$ , rate of fractional order system total mechanical

energy  $\mathbf{E} = \mathbf{E}_k + \mathbf{E}_p$  degradation is equal to negative sum of double Rayleigh function  $2\Phi$  and matrix product between velocity  $(\dot{x})$  and first partial derivative  $\frac{\partial \mathbf{P}_\alpha}{\partial (\mathfrak{D}_t^\alpha \{x\})}$  of generalized function of fractional order energy dissipation with respect to fractional order derivative  $\mathfrak{D}_t^\alpha \{x\}$ .

$$\frac{d\mathbf{E}}{dt} = -2\Phi - \sum_{k=1}^{k=n} \sum_{j=1}^{j=n} \dot{x}_k \frac{\partial \mathbf{P}_\alpha}{\partial (\mathfrak{D}_t^\alpha [x_j])}, \quad \text{for } \alpha \neq 0 \text{ and } 0 < \alpha \leq 1 \quad (1)$$

For system with one degree of freedom previous relation (10) take the following form:

$$\frac{d\langle E_{kinet} + E_{pot} \rangle}{dt} = -2\Phi(\dot{u}) + Q_{frac}(\mathfrak{D}_t^\alpha [u])\dot{u} \quad 0 < \alpha \leq 1 \quad (2)$$

or

$$\frac{d\mathbf{E}}{dt} = -2\Phi(\dot{u}) - \frac{\partial \mathbf{P}(\mathfrak{D}_t^\alpha [u])}{\partial \langle \mathfrak{D}_t^\alpha [u] \rangle} \dot{u} = -b\dot{u}^2 - b_\alpha \mathfrak{D}_t^\alpha [u] \dot{u} \quad 0 < \alpha \leq 1 \quad (3)$$

**Theorem 2:** For a class of fractional order no conservative system dynamic, with  $n$  degrees of freedom, and defined by: matrix of inertia properties  $\mathbf{A} = (a_{kj})_{\substack{\downarrow k=1,2,3,\dots,n \\ \rightarrow j=1,2,3,\dots,n}}$ , matrix of rigidity properties  $\mathbf{C} = (c_{kj})_{\substack{\downarrow k=1,2,3,\dots,n \\ \rightarrow j=1,2,3,\dots,n}}$ , matrix of viscoelastic creep fractional order properties  $\mathbf{C}_\alpha = (c_{\partial,kj})_{\substack{\downarrow k=1,2,3,\dots,n \\ \rightarrow j=1,2,3,\dots,n}}$  and matrix of viscoic linear properties  $\mathbf{B} = (b_{kj})_{\substack{\downarrow k=1,2,3,\dots,n \\ \rightarrow j=1,2,3,\dots,n}}$ , with properties that both side product by modal matrix  $\mathbf{R} = (\{K_{nk}^s\}) = (K_{nk}^s)_{\substack{\downarrow k=1,2,3,\dots,n \\ \rightarrow s=1,2,3,\dots,n}}$  of corresponding linear system produce all system matrix in diagonal form:  $\mathfrak{A} = \mathbf{R}'\mathbf{A}\mathbf{R} = \text{diag}(\tilde{a}_{ss})$ ,  $\mathfrak{C} = \mathbf{R}'\mathbf{C}\mathbf{R} = \text{diag}(\tilde{c}_{ss})$ ,  $\mathfrak{B} = \mathbf{R}'\mathbf{B}\mathbf{R} = \text{diag}(\tilde{b}_{ss})$ ,  $\mathfrak{C}_\alpha = \mathbf{R}'\mathbf{C}_\alpha\mathbf{R} = \text{diag}(\tilde{c}_{(\alpha)ss})$ ,

then rate of each system independent eigen main fractional order mode total mechanical energy  $\mathbf{E}_s = \mathbf{E}_{kin,s} + \mathbf{E}_{pot,s}$  degradation is equal to negative sum of double Rayleigh function  $2\Phi_s$  and matrix product between velocity  $\xi_s$  and first partial derivative  $\frac{\partial \mathbf{P}_\alpha}{\partial (\mathfrak{D}_t^\alpha [\xi_s])}$  of generalized function of fractional order energy dissipation with respect to fractional order derivative  $\mathfrak{D}_t^\alpha [\xi_s]$ :

$$\frac{d\mathbf{E}_s}{dt} = -2\Phi_s - \xi_{s,s} \frac{\partial \mathbf{P}_\alpha}{\partial (\mathfrak{D}_t^\alpha [\xi_s])}, \quad \text{for } \alpha \neq 0, 0 < \alpha < 1, s = 1, 2, 3, \dots, n, \quad (4)$$

or in the form:

$$\frac{d\mathbf{E}_s}{dt} = -2\Phi_s - \tilde{c}_{\alpha,ss} \xi_s \mathfrak{D}_t^\alpha [\xi_s], \quad \text{for } \alpha \neq 0, 0 < \alpha \leq 1, s = 1, 2, 3, \dots, n \quad (5)$$

Hybrid system contains multi deformable bodies (beams, plates or membranes), same boundary conditions, coupled by discrete continuum layers. Discrete continuum layers are built by standard elastic and inertia properties and fractional order elements homogeneously distributed between each of two adjacent deformable bodies. During the dynamics of deformable bodies in transversal direction each of standard elastic, and inertia, and fractional order elements obtain extension or compression equal to difference between two displacements of the corresponding body points for which are coupled its ends:  $\Delta w_{k+1,k}(x, y, t) = w_{k+1}(x, y, t) - w_k(x, y, t)$  for plates and membranes, and  $\Delta w_{k+1,k}(x, t) = w_{k+1}(x, t) - w_k(x, t)$  for beams and belts. Energy analysis of dynamics of definrd multi-deformable body system with elastic, and translator ind rotator inertia properties, and fractional order discrete continuum layers is presented. Sries of theorems are defined and proofed. One of theorem is:

**Theorem 3.** Generalized forces  $Q_{w_k}^{elem-sloja}$  and  $Q_{w_{k+1}}^{elem-sloja}$  of interaction between two deformable bodies coupled by standard discrete continuum layer with known kinetic  $\mathbf{E}_k^{elem-sloja}$  and potential  $\mathbf{E}_p^{elem-sloja}$  energies and known Rayleigh function of energy dissipation  $\Phi^{elem-sloja}$  and generalized function of fractional order element energy dissipation in the form:

$\Phi_{0<\alpha<1}^{elem-layer} = \frac{1}{2} c_{0<\alpha<1(k,k+1)} \{ \mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)] \}^2$ , where  $\mathfrak{D}_t^\alpha [\bullet]$  is fractional order differential operator of the  $\alpha^{th}$  derivative with respect to time  $t$  in the following form:  $\mathfrak{D}_t^\alpha [\bullet] = \frac{d^\alpha [\bullet]}{dt^\alpha} = \frac{1}{\Gamma(1-\alpha)} \frac{d}{dt} \int_0^t \frac{[\bullet]}{(t-\tau)^\alpha} d\tau$

$\Gamma(1-\alpha)$  is Euler Gama function,  $c_{\alpha(k,k+1)}$  are rigidity coefficients expressing fractional order dissipation properties, and  $\alpha$  a rational number between 0 and 1,  $0 < \alpha < 1$ , expressing dissipation properties of standard fractional order element, for generalized coordinates  $w_k(x, y, t)$  and  $w_{k+1}(x, y, t)$  displacement of deformable bodies at the point of contacts with discrete continuum elastic, inertia and fractional order layer are in the following forms:

$$Q_{w_k}^{elem-layer} = - \left\langle \frac{d}{dt} \frac{\partial \mathbf{E}_k^{elem-layer}}{\partial \left( \frac{\partial w_k(x, y, t)}{\partial t} \right)} - \frac{\partial \mathbf{E}_k^{elem-layer}}{\partial w_k(x, y, t)} \right\rangle - \frac{\partial \mathbf{E}_p^{elem-layer}}{\partial w_k(x, y, t)} - \frac{\partial \Phi^{elem-layer}}{\partial \left( \frac{\partial w_k(x, y, t)}{\partial t} \right)} - \frac{\partial \Phi_{0<\alpha<1}^{elem-layer}}{\partial (\mathfrak{D}_t^\alpha [w_k(x, y, t)])} = Q_{w_k}^{elem-def.body} \quad (6)$$

$$Q_{w_{k+1}}^{elem-layer} = - \left\langle \frac{d}{dt} \frac{\partial \mathbf{E}_k^{elem-layer}}{\partial \left( \frac{\partial w_{k+1}(x, y, t)}{\partial t} \right)} - \frac{\partial \mathbf{E}_k^{elem-layer}}{\partial w_{k+1}(x, y, t)} \right\rangle - \frac{\partial \mathbf{E}_p^{elem-layer}}{\partial w_{k+1}(x, y, t)} - \frac{\partial \Phi^{elem-layer}}{\partial \left( \frac{\partial w_{k+1}(x, y, t)}{\partial t} \right)} - \frac{\partial \Phi_{0<\alpha<1}^{elem-layer}}{\partial (\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t)])} = Q_{w_{k+1}}^{elem-def.body}$$

expressed by energies and energy dissipation which posses discrete continuum layer.

Other theprems are related to the change: \* of total mechanical energy of one eigen amplitude mode and generalized function of fractional order energy dissipation; \* of a total mechanical energy of a eigen time mode of eihrn time function correspond to one eigen amplitude mode. Transiet of enegy between defrmable bodies in the hybrid system is analyzed.

**Theorem 4.** Change of total mechanicale energy of the multy bory fractional order system dynamics is equal to the power of dissipative forces and fractional order dissipative forces work along corresponding system displacements:

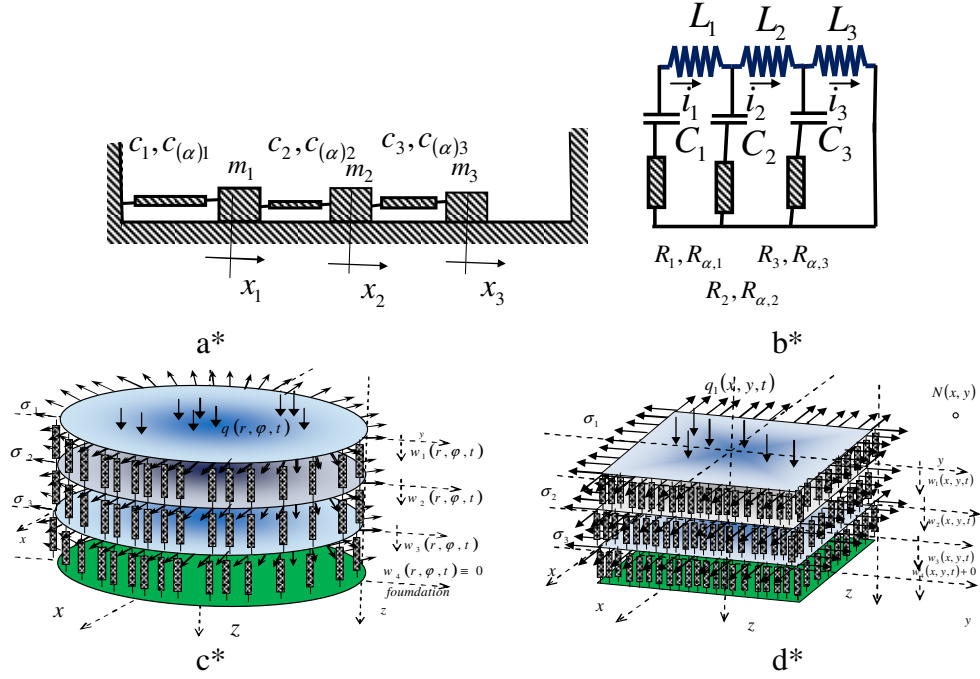
$$\frac{d(\mathbf{E}_{k,bodies} + \mathbf{E}_{p,bodies})}{dt} + \frac{d(\mathbf{E}_{k,layers} + \mathbf{E}_{p,layers})}{dt} = -2\Phi_{layers} - \sum_{\substack{k=1 \\ w_k(x,y,t)=0}}^3 \frac{\partial \Phi_{0<\alpha\leq 1} (\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)])}{\partial (\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)])} (\dot{w}_{k+1}(x, y, t) - \dot{w}_k(x, y, t)) \quad (7)$$

Where

$$\mathbf{P}_{(0<\alpha<1)k,k+1} = \frac{\partial \Phi_{0<\alpha\leq 1} (\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)])}{\partial (\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)])} (\dot{w}_{k+1}(x, y, t) - \dot{w}_k(x, y, t)) \quad (8)$$

power of fractional order dissipative forces of a discrete continuum layer between two deformable bodies (plates,, or membranes, or beams) and along displacements of upper  $w_k(x, y, t)$  and lower  $w_{k+1}(x, y, t)$  body (plate or membrane); and  $\mathfrak{D}_t^\alpha [\bullet]$  is fractional order differential operator of the  $\alpha^{th}$  derivative with respect to time  $t$  in the following form[4-11]:

$$\mathfrak{D}_t^\alpha [\bullet] = \frac{d^\alpha [\bullet]}{dt^\alpha} = \frac{1}{\Gamma(1-\alpha)} \frac{d}{dt} \int_0^t \frac{[\bullet]}{(t-\tau)^\alpha} d\tau \quad (9)$$



**Figure1.** Qualitative and mathematical analogous fractional order chains: a\* mechanical fractional order chain system and b\* electrical fractional order chain system as well as ; c\* multi circular membrane and d\* multi rectangular membrane system on the fractional order discrete continuum foundation.

**Table 1.** Qualitative and mathematical analogous fractional order system energies: a\* mechanical fractional order system and b\* electrical fractional order system

	Kinetic energy	Potential energy	Generalized function of fractional order energy dissipation	Energy relations in fractional order system
a*	For mass particles $2E_k = (\dot{x})A\{\dot{x}\}$ $2E_k = \sum_{s=1}^{s=n} \dot{\eta}_s^2$ $\eta_s, s = 1, 2, 3, \dots, n$ eigen normal coordinates (modes) of displacements	For linear elastic springs $2E_p = (x)C\{x\}$ $2E_p = \sum_{s=1}^{s=n} \omega_s^2 \eta_s^2$	Power of fractional order dissipative forces in standard fractional order elements $2P_{\alpha \neq 0} = (\mathfrak{D}_t^\alpha \{x\})C_\alpha \{\mathfrak{D}_t^\alpha \{x\}\}$ for $\alpha \neq 0, 0 < \alpha < 1$ $2P_\alpha = \sum_{s=1}^{s=n} \omega_{(\alpha),s}^2 (\mathfrak{D}_t^\alpha [\eta_s])^2$ for $\alpha \neq 0, 0 < \alpha < 1$	System total mechanical energy rate $\frac{dE}{dt} = -2\Phi - \sum_{k=1}^{k=n} \sum_{j=1}^{j=n} \dot{x}_k \frac{\partial P_\alpha}{\partial (\mathfrak{D}_t^\alpha [x_j])}$ for $\alpha \neq 0, 0 < \alpha < 1$ Eigen main fractional order independent mode total mechanical energy rate $\frac{dE_s}{dt} = -2\Phi_s - \dot{\xi}_{ss} \frac{\partial P_\alpha}{\partial (\mathfrak{D}_t^\alpha [\xi_s])}$ for $\alpha \neq 0, 0 < \alpha < 1, s = 1, 2, 3, \dots, n$
b*	For inductors $2E_k = (\dot{q})L\{\dot{q}\}$ $2E_k = \sum_{s=1}^{s=n} \dot{\eta}_s^2$ $\eta_s, s = 1, 2, 3, \dots, n$ eigen normal coordinates (modes) of electricity	For linear capacitors $2E_p = (q)C^* \{q\}$ $2E_p = \sum_{s=1}^{s=n} \omega_s^2 \eta_s^2$	Power of fractional order dissipative electrical voltage in standard fractional order resistors $2P_{\alpha \neq 0} = (\mathfrak{D}_t^\alpha \{q\})R_\alpha \{\mathfrak{D}_t^\alpha \{q\}\}$ for $\alpha \neq 0, 0 < \alpha < 1$ $2P_\alpha = \sum_{s=1}^{s=n} \omega_{(\alpha),s}^2 (\mathfrak{D}_t^\alpha [\eta_s])^2$ for $\alpha \neq 0, 0 < \alpha < 1$	System total electrical energy rate $\frac{dE}{dt} = -2\Phi - \sum_{k=1}^{k=n} \sum_{j=1}^{j=n} \dot{x}_k \frac{\partial P_\alpha}{\partial (\mathfrak{D}_t^\alpha [x_j])}$ for $\alpha \neq 0, 0 < \alpha < 1$ Eigen main fractional order independent mode total electrical energy rate $\frac{dE_s}{dt} = -2\Phi_s - \dot{\xi}_{ss} \frac{\partial P_\alpha}{\partial (\mathfrak{D}_t^\alpha [\xi_s])}$ for $\alpha \neq 0, 0 < \alpha < 1, s = 1, 2, 3, \dots, n$

$\Gamma(1-\alpha)$  is Euler Gamma function, and  $c_{0(k,k+1)}$  and  $c_{\alpha(k,k+1)}$  are rigidity coefficients – momentary (expressing ideal elastic properties) and prolonged one (expressing fractional order dissipation properties), and  $\alpha$  a rational number between 0 and 1,  $0 < \alpha < 1$ , expressing elastic and dissipation properties of standard fractional order element.  $\tilde{\Phi}_{0 < \alpha < 1} = \frac{1}{2} c_{0 < \alpha < 1(k,k+1)} \{\mathfrak{D}_t^\alpha [w_{k+1}(x, y, t) - w_k(x, y, t)]\}^2$  generalized function of fractional order discrete continuum layer energy dissipation for  $0 < \alpha \leq 1$ .

**Acknowledgement.** Parts of this research were supported by the Ministry of Sciences of Republic Serbia through Mathematical Institute SANU Belgrade Grants OI 174001 "Dynamics of hybrid systems with complex structures. Mechanics of materials", Faculty of Mechanical Engineering University of Niš.

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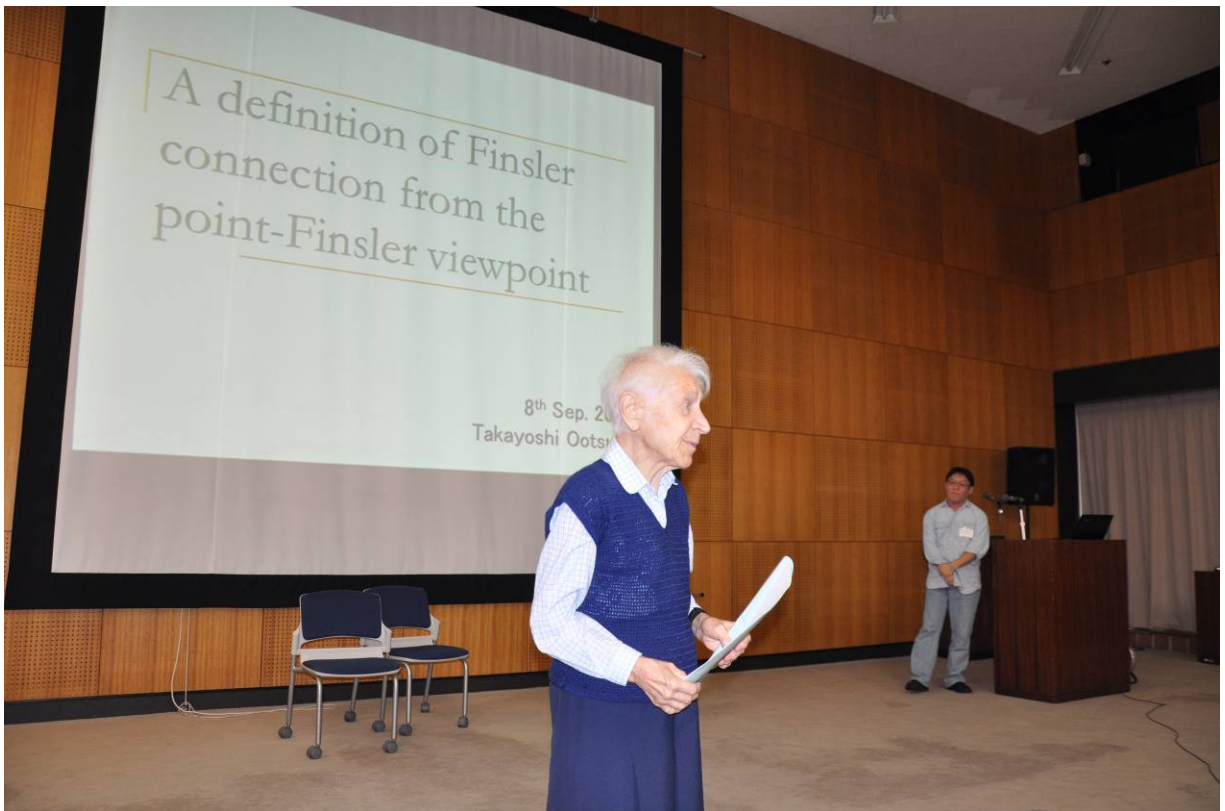
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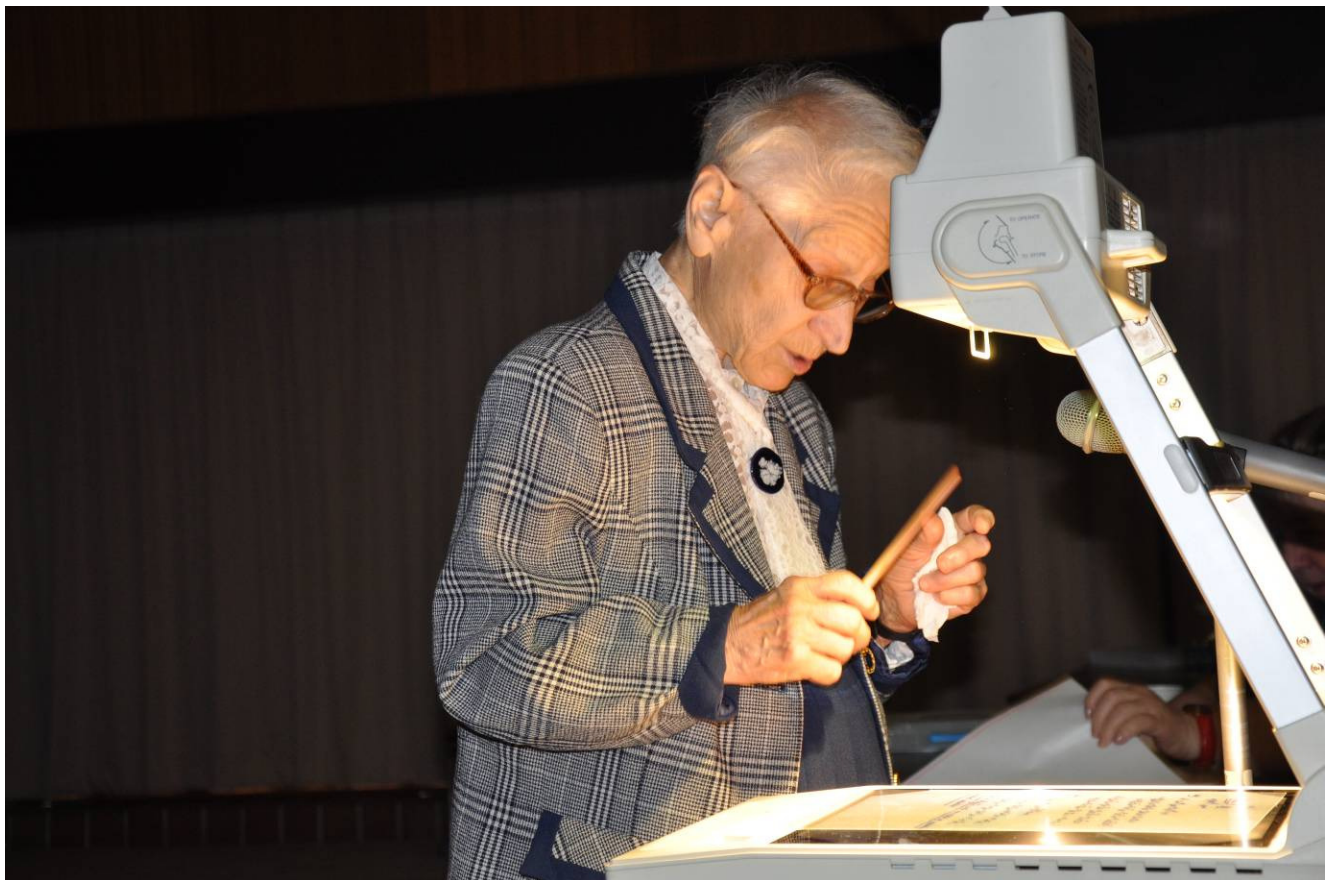




THE 14<sup>th</sup> INTERNATIONAL CONFERENCE OF TENSOR SOCIETY ON DIFFERENTIAL GEOMETRY AND ITS APPLICATIONS, AND INFORMATICS BESIDES Organized by Tensor Society and University of Tsukuba for mutual Progress, Held at Tsukuba, on Japan, Sept. 7-12, 2015

















IMPALA  
KUMODRASKA 10  
BEOGRAD  
TELEPHONE: 381 11 2497 882  
FAX: 381 11 309 6428  
EMAIL: [INFO@IMPALAYU.COM](mailto:INFO@IMPALAYU.COM)

BOOKING REF: YI4J62  
DATE: 28 JULY 2015

**HEDRIH/KATICA MRS**

**FLIGHT JU 310 - AIR SERBIA** SUN 06 SEPTEMBER 2015

DEPARTURE: **BELGRADE, RS (NIKOLA TESLA), TERMINAL 2** 06 SEP 06:40  
ARRIVAL: **PARIS, FR (CHARLES DE GAULLE), TERMINAL 2D -** 06 SEP 09:15  
AEROGARE 2 TERMINAL D  
FLIGHT BOOKING REF: JU/YI4J62 LAST CHECK IN TIME: 05:55  
RESERVATION CONFIRMED, ECONOMY (L) DURATION: 02:35

BAGGAGE ALLOWANCE: 1PC  
SEAT: **05B CONFIRMED FOR HEDRIH/KATICA MRS**  
MEAL: MEAL  
**WHEELCHAIR-FOR RAMP CONFIRMED**  
NON STOP BELGRADE TO PARIS  
OPERATED BY: AIR SERBIA, JU  
EQUIPMENT: AIRBUS INDUSTRIE A320-100/200

**FLIGHT AF 272 - AIR FRANCE** SUN 06 SEPTEMBER 2015

DEPARTURE: **PARIS, FR (CHARLES DE GAULLE), TERMINAL 2E -** 06 SEP 11:05  
AEROGARE 2 TERMINAL E  
ARRIVAL: **TOKYO, JP (TOKYO INTL HANEDA), TERMINAL I -** 07 SEP 06:00  
INTERNATIONAL TERMINAL  
FLIGHT BOOKING REF: AF/YI4J62 LAST CHECK IN TIME: 10:05  
RESERVATION CONFIRMED, ECONOMY (T) DURATION: 11:55

BAGGAGE ALLOWANCE: 1PC  
SEAT: **38K CONFIRMED FOR HEDRIH/KATICA MRS**  
MEAL: SNACK/MEAL  
**WHEELCHAIR-FOR RAMP CONFIRMED**  
NON STOP PARIS TO TOKYO  
OPERATED BY: AIR FRANCE, AF  
EQUIPMENT: BOEING 777-200/200ER

**FLIGHT AZ 787 - ALITALIA S.A.I. S.P.A.** SUN 20 SEPTEMBER 2015

DEPARTURE: **TOKYO, JP (NARITA INTL), TERMINAL 1** 20 SEP 13:00  
ARRIVAL: **MILAN, IT (MALPENSA), TERMINAL 1** 20 SEP 18:30  
FLIGHT BOOKING REF: AZ/MXR7SR  
RESERVATION CONFIRMED, ECONOMY (X) DURATION: 12:30

BAGGAGE ALLOWANCE: 2PC  
SEAT: **23K CONFIRMED FOR HEDRIH/KATICA MRS**  
**WHEELCHAIR-FOR RAMP CONFIRMED**  
NON STOP TOKYO TO MILAN  
OPERATED BY: ALITALIA S.A.I. S.P.A., AZ  
EQUIPMENT: BOEING 777-200/200ER

**FLIGHT AZ 7076 - ALITALIA S.A.I. S.P.A.** SUN 20 SEPTEMBER 2015

DEPARTURE: **MILAN, IT (MALPENSA), TERMINAL 1** 20 SEP 20:55  
ARRIVAL: **BELGRADE, RS (NIKOLA TESLA)** 20 SEP 22:35  
FLIGHT BOOKING REF: AZ/MXR7SR  
RESERVATION CONFIRMED, ECONOMY (X) DURATION: 01:40

BAGGAGE ALLOWANCE: 2PC  
WHEELCHAIR-FOR RAMP CONFIRMED

NON STOP MILAN TO BELGRADE  
OPERATED BY:  
EQUIPMENT:

AIR SERBIA, JU 545  
AIRBUS INDUSTRIE A319

FLIGHT TICKET(S)

TICKET: **AF/ETKT 057 9340299346-47 FOR HEDRIH/KATICA MRS**

GENERAL INFORMATION

CHECK YOUR TRIP ONLINE

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T. Kawaguchi<tensor-ns@nifty.ne.jp>;

**From:** [T. Kawaguchi](#)  
**Sent:** Monday, August 31, 2015 11:50 PM  
**To:** [Katica Hedrih](#)  
**Cc:** [T. Kawaguchi](#)  
**Subject:** Re: Address in Japan

Tsukuba, Sept. 1, 2015

Dear Professors Hedrih and Prvanovic,

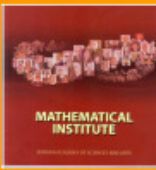
Thank you for your kind message. I and my wife Akemi are good health.  
In Tokyo, we have arranged that you with your grand daughter and Mrs. Prvanovic together will stay in my apartment at Tokyo:  
**Komagome 1-3-5-302, Toshima-ku, Tokyo.**  
**Tel. 81- 03-3947-3910, Mobil Phone: 090-9150-4681 (Tomoaki), 090-8486-7413 (Akemi),**  
**81 means Japanese country code, 03 means Tokyo code.**  
**My apartment is not so large, but it is in center of Tokyo, and very near Komagome Station (JR rail way, Yamanote line).**  
During conference, you can put big laggage etc.

**In Tsukuba, we also arranged Guest House of Univ. of Tsukuba,**  
**Room No. 407, for Mrs. Prvanovic, Tel. 029-853-8707 (direct),**  
**Room No. 408(twin), for you and Grand daughter, Tel. 029-853-8708 (direct)**  
**Room No. 406 (twin), for I and my brother, Tel. 029-853-8706 (direct).**

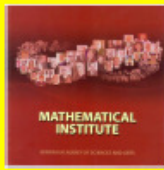
On 7th Sept., my wife Akemi will pick up you and Prof. Prvanovic at Tokyo Haneda airport, after then will go to my apartment. After some rest there, evening, **Prof. H. Endo and Prof. T. Kashiwada** will guide and accompany all member to Univ. of Tsukuba.

All member: Prof. Prvanovic, Prof. Hedrih and Miss Mihaela, Dr. Zerrin Senturk.

Looking forward to seeing soon, Sincerely yours,  
Tomoaki KAWAGUCHI and Akemi KAWAGUCHI



# Tensor Calculus in Yugoslavia and Serbia: Academicina Tatomir P. Andjelić (1903-1993) and Prof. Dr. Ing. Dipl. Math. Danilo P. RAŠKOVIĆ (1910-1985)



**Hedrih (Stevanović) R. Katica**  
Mathematical Institute SANU Belgrade,  
and Faculty of Mechanical Engineering University of Niš, Serbia



*Машеи Баи зва  
зага навири Анђелић  
за црвену.*  
\*  
*Катинге, момаи ве  
сениабуре у Маи. мови.  
за мене, јогаи Баи  
лишари о рудбаиури  
Крепути.*  
Маша Баи,  
Београд



*Prof. P. Kraussner  
i Max von Tomatis*  
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Mit 100 Abbildungen  
Spekter-Verlag Berlin Heidelberg New York 1968

**II. Tenzorkalkül selbst Anzeiger**  
Von Tatomir P. Andjelić, Beograd  
Tenzorkalkül  
§ 1. Punkt. Raum. Koordinatensystem.  
Koordinatentransformation  
Ein Matrizenpaar  $(g_{ij}, g^{ij})$  der 3. Variablen  $x^i, x^j, \dots, x^n$  ist sich als ein Paar in 3-dimensionalen Raum  $V_3$  denken. Man nennt das Paar von Matrizen  $g_{ij}, g^{ij}$  die Krümmungstensor-Punkte (bezügig auf die Koordinaten  $x^i, x^j, \dots, x^n$ ). Die beiden diese Variablen als einzigen reellen Werte, so läßt die sich diese Werte beliebige Menge von Punkten vom Raum  $V_3$ , die über sich reelle Funktionen gesetzt sind.  
Metrische Formel nennt unter dem Namen  $F_1$  die partielle Differentialrechnung Raum  $V_3$ , eine entsprechende Bildung aus. Wie bekannt, werden unter diesem Punkt zu unterschiedlichen Ereignissen mittels verschiedener Koordinatensysteme bestimmt. Man verwendet dabei vollständige oder schiefwinklige, geodetische oder verdrillte Koordinaten, usw. In dem letzten oder im die ersten Hilfsmittel im allgemeinen Systeme in seine Hilfe jedoch erweitert sich bei der klassischen Behandlung technischer und physikalischer Probleme Verwendung eines 3-dimensionalen Raumes als nicht topolog. so daß es hier auf die Erweiterung der entsprechenden Begriffe und die Möglichkeit der geometrischen Deutung in abstrakter Raum nicht verzichten sollte.  
Ausgabe über gewisse qualitative bestimmbare Eigenschaften in Natur und Technik werden hat immer als Ausgangs über eine Menge von physikalischen, mechanischen, physikalischen) in geeigneten Fällen gelten.  
[1]  $[g] = [g^i_j]$   
[2]  $g^i_j = g^j_i$   $g^i_i = 1, 2, \dots, n$

Beograd, 20.X.1984.  
Draga Katica,  
Evalu Vas na poslatoj kopiji prihvatanja recenzije kolega recenzentata. Taj akt i onaj prethodni kopirao sam i prilozicu rukopisu, kako traži "šaušna knjiga". Sada su oni mnogo naušneti sretnijem sa sajan knjiga, pa čeno pregled rukopisa i sve što ide us to ostaviti sa početak novembra. Dao sam orteše ing. Viliđiu, pa će i oni biti verovatno g gotovi.  
Kada sam bio kod "šaušne knjige" uspeo sam da od njih dobijem jedan primerak "Zbirke sadataka" /is njahnova biblioteka/. Tako smo sređili i **ovu stvar** da Vas ne mušim više, ni da solite Milku u moje ime. Priznajem da sam Vas mnogo nagajvio sa ovim poslovima, ali šta čete, Vi ste mi jedina uzdanica i pomoć. Još jednom veliko Van hvala.  
Kako ste Vi? Imate li mnogo posla? Sigurno, da imate, štola je takva, nikad mira. Kako je gospodin Vlacimir je već veliki sukak. Poljubite ga.  
Prinite mnogo pozdrava od moje supruge.  
Uz zahvalnost, mnogo, mnogo toplih pozdrava  
Vaš  
*D. Rašković*  
/prof. Rašković/

**ТРОПСКА  
ЕЛЕКТРОНИКА**  
ОСНОВНИ ТЕНЗОРСКА РАЧУНА

*Kočinje Katine,  
Đao mi je mađ ne  
mađ stevanij HAU  
Hny u ga Bugina  
kako je spetena  
seba prof. Mitaševića  
sa šaušna knjigama.  
Da nisam istogrekn,  
đvoas im o upotreb  
štoj razgovora.  
Kožj, ališje uvažj  
Mitaševića ka  
Baš  
7. aprila 1984. g. B. B.*

**APOLLO 15**  
THE FOURTH TROUBLE  
WITH MOON WALKS FROM THE  
CAMERA OF Apollo 15  
**Preliminary  
Science  
Report**  
NATIONAL AERONAUTICS  
AND SPACE ADMINISTRATION

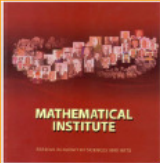
Beograd, 16.08.'84  
Draga Katica,  
Juče sam bio kod "šaušne knjige", pre nisan mogao, jer su bili na odmoru. Tako su kolege Andelić i Bršić bili vrlo agilni, referat /recenzija/ je morao da šeka. Kao što vidite recenzija je perfektna. Rukopis se mnogo sviđa kolegi Bršiću. Prof. Andelića nisam video, bio je malo bolestan. Sada je sve u redu.  
"šaušna knjiga" je sadržala rukopis radi detaljnog pregleda i voljna je da ga štampa u 2000 primeraka /uobičajeni ekonomsko opravdani tiraž/. Litografisanje ne dolazi u obzir zbog vrlo komplikovanog teksta i nerentabilnosti.  
Oni smatraju  
1. da MF u Nišu treba da plati honorar recenzentima,  
2. da pisac preda orteše u tušu na pusu ili hameru radi kliširanja,  
3. da novčana pomoć MF iz Niša noše da se ostvari na dva načina  
a/ dodeljivanjem KNjisi besprovatne sume novca radi smanjenja proćajne cene knjige,  
b/ zagarantovanog otkupa izvesne količine knjige.  
Oni će da izvrše kalkulaciju, pa mole da ih MF izvesti. Obaveštenje je najbolje poslati MK.  
Kako ste Vi i Vaši? Jeste li se dobro odmorili? Mnogi se hvala kako im je bilo dobro u Grčkoj, Šurij, i izvijavaju se sa eventualne greške. Še-lin da pošaljem dokumenta.  
Briđaan pozdrav  
*D. Rašković*  
/prof. Rašković/

*Prof. Rašković*  
[Handwritten notes and signatures]

**Assessment Report**  
[Handwritten notes and signatures]



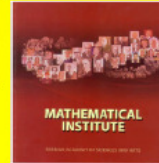




# Tensor Society and Journal Tensor

Professor Dr. Tomoaki Kawaguchi,

President of Tensor Society and Edito-in-Chief



Serbian Scientific Society



Hedrih (Stevanović) R. Katica

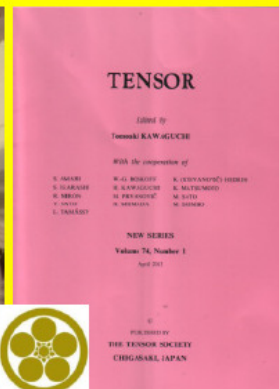
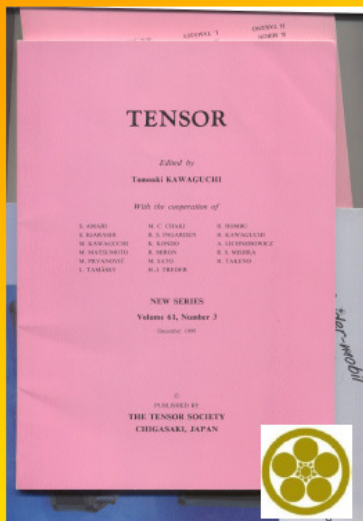
Mathematical Institute SANU Belgrade,  
and Faculty of Mechanical Engineering University of Niš, Serbia



Professor Dr. Tomoaki KAWAGUCHI



THE 6th INTERNATIONAL CONFERENCE OF TENSOR SOCIETY, Takuba, Japan, Aug. 5-8, 2002  
On occasion of the Anniversary of "Akitsune Kawaguchi's 100 years birth"



Tensor Society Conference, Tokyo, 7-12<sup>th</sup> September 2015

